

NAG Library Routine Document

G08ACF

Note: before using this routine, please read the Users' Note for your implementation to check the interpretation of ***bold italicised*** terms and other implementation-dependent details.

1 Purpose

G08ACF performs the Median test on two independent samples of possibly unequal size.

2 Specification

```
SUBROUTINE G08ACF (X, N, N1, W, I1, I2, P, IFAIL)
  INTEGER          N, N1, I1, I2, IFAIL
  REAL (KIND=nag_wp) X(N), W(N), P
```

3 Description

The Median test investigates the difference between the medians of two independent samples of sizes n_1 and n_2 , denoted by:

$$x_1, x_2, \dots, x_{n_1}$$

and

$$x_{n_1+1}, x_{n_1+2}, \dots, x_n,$$

where $n = n_1 + n_2$.

The hypothesis under test, H_0 , often called the null hypothesis, is that the medians are the same, and this is to be tested against the alternative hypothesis H_1 that they are different.

The test proceeds by forming a 2×2 frequency table, giving the number of scores in each sample above and below the median of the pooled sample:

	Sample 1	Sample 2	Total
Scores < pooled median	i_1	i_2	$i_1 + i_2$
Scores \geq pooled median	$n_1 - i_1$	$n_2 - i_2$	$n - (i_1 + i_2)$
Total	n_1	n_2	n

Under the null hypothesis, H_0 , we would expect about half of each group's scores to be above the pooled median and about half below, that is, we would expect i_1 to be about $n_1/2$ and i_2 to be about $n_2/2$.

G08ACF returns:

- the frequencies i_1 and i_2 ;
- the probability, p , of observing a table at least as 'extreme' as that actually observed, given that H_0 is true. If $n < 40$, p is computed directly ('Fisher's exact test'); otherwise a χ^2_1 approximation is used (see G01AFF).

H_0 is rejected by a test of chosen size α if $p < \alpha$.

4 References

Siegel S (1956) *Non-parametric Statistics for the Behavioral Sciences* McGraw-Hill

5 Arguments

- 1: $X(N)$ – REAL (KIND=nag_wp) array *Input*
On entry: the first n_1 elements of X must be set to the data values in the first sample, and the next n_2 ($= N - n_1$) elements to the data values in the second sample.

- 2: N – INTEGER *Input*
On entry: the total of the two sample sizes, n ($= n_1 + n_2$).
Constraint: $N \geq 2$.

- 3: $N1$ – INTEGER *Input*
On entry: the size of the first sample n_1 .
Constraint: $1 \leq N1 < N$.

- 4: $W(N)$ – REAL (KIND=nag_wp) array *Workspace*

- 5: $I1$ – INTEGER *Output*
On exit: the number of scores in the first sample which lie below the pooled median, i_1 .

- 6: $I2$ – INTEGER *Output*
On exit: the number of scores in the second sample which lie below the pooled median, i_2 .

- 7: P – REAL (KIND=nag_wp) *Output*
On exit: the tail probability p corresponding to the observed dichotomy of the two samples.

- 8: $IFAIL$ – INTEGER *Input/Output*
On entry: $IFAIL$ must be set to 0, -1 or 1. If you are unfamiliar with this argument you should refer to Section 3.4 in How to Use the NAG Library and its Documentation for details.
For environments where it might be inappropriate to halt program execution when an error is detected, the value -1 or 1 is recommended. If the output of error messages is undesirable, then the value 1 is recommended. Otherwise, if you are not familiar with this argument, the recommended value is 0. **When the value -1 or 1 is used it is essential to test the value of $IFAIL$ on exit.**
On exit: $IFAIL = 0$ unless the routine detects an error or a warning has been flagged (see Section 6).

6 Error Indicators and Warnings

If on entry $IFAIL = 0$ or -1 , explanatory error messages are output on the current error message unit (as defined by X04AAF).

Errors or warnings detected by the routine:

$IFAIL = 1$

On entry, $N < 2$.

$IFAIL = 2$

On entry, $N1 < 1$,
or $N1 \geq N$.

IFAIL = -99

An unexpected error has been triggered by this routine. Please contact NAG.

See Section 3.9 in How to Use the NAG Library and its Documentation for further information.

IFAIL = -399

Your licence key may have expired or may not have been installed correctly.

See Section 3.8 in How to Use the NAG Library and its Documentation for further information.

IFAIL = -999

Dynamic memory allocation failed.

See Section 3.7 in How to Use the NAG Library and its Documentation for further information.

7 Accuracy

The probability returned should be accurate enough for practical use.

8 Parallelism and Performance

G08ACF is not threaded in any implementation.

9 Further Comments

The time taken by G08ACF is small, and increases with n .

10 Example

This example is taken from page 112 of Siegel (1956). The data relate to scores of ‘oral socialisation anxiety’ in 39 societies, which can be separated into groups of size 16 and 23 on the basis of their attitudes to illness.

10.1 Program Text

```

Program g08acfe

!      G08ACF Example Program Text

!      Mark 26 Release. NAG Copyright 2016.

!      .. Use Statements ..
      Use nag_library, Only: g08acf, nag_wp
!      .. Implicit None Statement ..
      Implicit None
!      .. Parameters ..
      Integer, Parameter          :: nin = 5, nout = 6
!      .. Local Scalars ..
      Real (Kind=nag_wp)          :: p
      Integer                     :: i1, i2, ifail, n, n1
!      .. Local Arrays ..
      Real (Kind=nag_wp), Allocatable :: w(:), x(:)
!      .. Executable Statements ..
      Write (nout,*) 'G08ACF Example Program Results'
      Write (nout,*)

!      Skip heading in data file
      Read (nin,*)

!      Read in problem size
      Read (nin,*) n, n1

```

```

        Allocate (x(n),w(n))

!      Read in data
        Read (nin,*) x(1:n)

!      Display title
        Write (nout,*) 'Median test'
        Write (nout,*)

!      Output data
        Write (nout,*) 'Data values'
        Write (nout,*)
        Write (nout,99999) '      Group 1  ', x(1:n1)
        Write (nout,*)
        Write (nout,99999) '      Group 2  ', x((n1+1):n)

!      Perform median test
        ifail = 0
        Call g08acf(x,n,n1,w,i1,i2,p,ifail)

!      Display results
        Write (nout,*)
        Write (nout,99998) i1, ' scores below median in group 1'
        Write (nout,99998) i2, ' scores below median in group 2'
        Write (nout,*)
        Write (nout,99997) '      Significance  ', p

99999 Format (1X,A,8F4.0,/, (14X,8F4.0))
99998 Format (1X,I6,A)
99997 Format (1X,A,F8.5)
        End Program g08acfe

```

10.2 Program Data

```

G08ACF Example Program Data
39 16                                :: N,N1
13.0  6.0 12.0  7.0 12.0  7.0 10.0
 7.0 10.0  7.0 10.0  7.0 10.0  8.0
 9.0  8.0 17.0  6.0 16.0  8.0 15.0
 8.0 15.0 10.0 15.0 10.0 14.0 10.0
14.0 11.0 14.0 11.0 13.0 12.0 13.0
12.0 13.0 12.0 12.0                :: End of X

```

10.3 Program Results

G08ACF Example Program Results

Median test

Data values

Group 1	13.	6.	12.	7.	12.	7.	10.	7.
	10.	7.	10.	7.	10.	8.	9.	8.
Group 2	17.	6.	16.	8.	15.	8.	15.	10.
	15.	10.	14.	10.	14.	11.	14.	11.
	13.	12.	13.	12.	13.	12.	12.	

13 scores below median in group 1
 6 scores below median in group 2

Significance 0.00088
