NAG Library Function Document

nag_pls_orth_scores_svd (g02lac)

1 Purpose

nag_pls_orth_scores_svd (g02lac) fits an orthogonal scores partial least squares (PLS) regression by using singular value decomposition.

2 Specification

```
#include <nag.h>
#include <nagg02.h>
void nag_pls_orth_scores_svd (Nag_OrderType order, Integer n, Integer mx,
     const double x[], Integer pdx, const Integer isx[], Integer ip,
     Integer my, const double y[], Integer pdy, double xbar[], double ybar[],
     Nag_ScalePredictor iscale, double xstd[], double ystd[], Integer maxfac,
     double xres[], Integer pdxres, double yres[], Integer pdyres,
     double w[], Integer pdw, double p[], Integer pdp, double t[],
     Integer pdt, double c[], Integer pdc, double u[], Integer pdu,
     double xcv[], double ycv[], Integer pdycv, NagError *fail)
```

3 Description

Let X_1 be the mean-centred n by m data matrix X of n observations on m predictor variables. Let Y_1 be the mean-centred n by r data matrix Y of n observations on r response variables.

The first of the k factors PLS methods extract from the data predicts both X_1 and Y_1 by regressing on t_1 a column vector of n scores:

$$\begin{aligned}\hat{X}_1 &= t_1 p_1^{\mathrm{T}} \\ \hat{Y}_1 &= t_1 c_1^{\mathrm{T}}, \quad \text{with } t_1^{\mathrm{T}} t_1 = 1,\end{aligned}$$

where the column vectors of m x-loadings p_1 and r y-loadings c_1 are calculated in the least squares sense:

$$\begin{aligned}p_1^{\mathrm{T}} &= t_1^{\mathrm{T}} X_1 \\ c_1^{\mathrm{T}} &= t_1^{\mathrm{T}} Y_1.\end{aligned}$$

The x-score vector $t_1 = X_1 w_1$ is the linear combination of predictor data X_1 that has maximum covariance with the y-scores $u_1 = Y_1 c_1$, where the x-weights vector w_1 is the normalised first left singular vector of $X_1^{\mathrm{T}} Y_1$.

The method extracts subsequent PLS factors by repeating the above process with the residual matrices:

$$\begin{aligned}X_i &= X_{i-1} - \hat{X}_{i-1} \\ Y_i &= Y_{i-1} - \hat{Y}_{i-1}, \quad i = 2, 3, \ldots, k,\end{aligned}$$

and with orthogonal scores:

$$t_i^{\mathrm{T}} t_j = 0, \quad j = 1, 2, \ldots, i-1.$$

Optionally, in addition to being mean-centred, the data matrices X_1 and Y_1 may be scaled by standard deviations of the variables. If data are supplied mean-centred, the calculations are not affected within numerical accuracy.

4 References

None.

5 Arguments

1: **order** – Nag_OrderType *Input*

On entry: the **order** argument specifies the two-dimensional storage scheme being used, i.e., row-major ordering or column-major ordering. C language defined storage is specified by **order** = Nag_RowMajor. See Section 2.3.1.3 in How to Use the NAG Library and its Documentation for a more detailed explanation of the use of this argument.

Constraint: **order** = Nag_RowMajor or Nag_ColMajor.

2: **n** – Integer *Input*

On entry: n, the number of observations.

Constraint: $\mathbf{n} > 1$.

3: **mx** – Integer *Input*

On entry: the number of predictor variables.

Constraint: $\mathbf{mx} > 1$.

4: **x**[dim] – const double *Input*

Note: the dimension, *dim*, of the array **x** must be at least

$\max(1, \mathbf{pdx} \times \mathbf{mx})$ when **order** = Nag_ColMajor;
$\max(1, \mathbf{n} \times \mathbf{pdx})$ when **order** = Nag_RowMajor.

Where $\mathbf{X}(i, j)$ appears in this document, it refers to the array element

$\mathbf{x}[(j-1) \times \mathbf{pdx} + i - 1]$ when **order** = Nag_ColMajor;
$\mathbf{x}[(i-1) \times \mathbf{pdx} + j - 1]$ when **order** = Nag_RowMajor.

On entry: $\mathbf{X}(i, j)$ must contain the ith observation on the jth predictor variable, for $i = 1, 2, \ldots, \mathbf{n}$ and $j = 1, 2, \ldots, \mathbf{mx}$.

5: **pdx** – Integer *Input*

On entry: the stride separating row or column elements (depending on the value of **order**) in the array **x**.

Constraints:

if **order** = Nag_ColMajor, $\mathbf{pdx} \geq \mathbf{n}$;
if **order** = Nag_RowMajor, $\mathbf{pdx} \geq \mathbf{mx}$.

6: **isx**[**mx**] – const Integer *Input*

On entry: indicates which predictor variables are to be included in the model.

isx$[j-1] = 1$
The jth predictor variable (with variates in the jth column of X) is included in the model.

isx$[j-1] = 0$
Otherwise.

Constraint: the sum of elements in **isx** must equal **ip**.

7: **ip** – Integer *Input*

On entry: m, the number of predictor variables in the model.

Constraint: $1 < \mathbf{ip} \leq \mathbf{mx}$.

8: **my** – Integer *Input*

On entry: r, the number of response variables.

Constraint: **my** ≥ 1.

9: **y**[dim] – const double *Input*

Note: the dimension, *dim*, of the array **y** must be at least

$\max(1, \mathbf{pdy} \times \mathbf{my})$ when **order** = Nag_ColMajor;
$\max(1, \mathbf{n} \times \mathbf{pdy})$ when **order** = Nag_RowMajor.

Where $\mathbf{Y}(i, j)$ appears in this document, it refers to the array element

y$[(j-1) \times \mathbf{pdy} + i - 1]$ when **order** = Nag_ColMajor;
y$[(i-1) \times \mathbf{pdy} + j - 1]$ when **order** = Nag_RowMajor.

On entry: $\mathbf{Y}(i, j)$ must contain the ith observation for the jth response variable, for $i = 1, 2, \ldots,$ **n** and $j = 1, 2, \ldots,$ **my**.

10: **pdy** – Integer *Input*

On entry: the stride separating row or column elements (depending on the value of **order**) in the array **y**.

Constraints:

if **order** = Nag_ColMajor, **pdy** $\geq$ **n**;
if **order** = Nag_RowMajor, **pdy** $\geq$ **my**.

11: **xbar**[**ip**] – double *Output*

On exit: mean values of predictor variables in the model.

12: **ybar**[**my**] – double *Output*

On exit: the mean value of each response variable.

13: **iscale** – Nag_ScalePredictor *Input*

On entry: indicates how predictor variables are scaled.

iscale = Nag_PredStdScale
Data are scaled by the standard deviation of variables.

iscale = Nag_PredUserScale
Data are scaled by user-supplied scalings.

iscale = Nag_PredNoScale
No scaling.

Constraint: **iscale** = Nag_PredNoScale, Nag_PredStdScale or Nag_PredUserScale.

14: **xstd**[**ip**] – double *Input/Output*

On entry: if **iscale** = Nag_PredUserScale, **xstd**$[j-1]$ must contain the user-supplied scaling for the jth predictor variable in the model, for $j = 1, 2, \ldots,$ **ip**. Otherwise **xstd** need not be set.

On exit: if **iscale** = Nag_PredStdScale, standard deviations of predictor variables in the model. Otherwise **xstd** is not changed.

15: **ystd**[**my**] – double *Input/Output*

On entry: if **iscale** = Nag_PredUserScale, **ystd**$[j-1]$ must contain the user-supplied scaling for the jth response variable in the model, for $j = 1, 2, \ldots,$ **my**. Otherwise **ystd** need not be set.

On exit: if **iscale** = Nag_PredStdScale, the standard deviation of each response variable. Otherwise **ystd** is not changed.

16: **maxfac** – Integer *Input*

On entry: k, the number of latent variables to calculate.

Constraint: $1 \leq$ **maxfac** $\leq$ **ip**.

17: **xres**$[dim]$ – double *Output*

Note: the dimension, *dim*, of the array **xres** must be at least

$\max(1, \mathbf{pdxres} \times \mathbf{ip})$ when **order** = Nag_ColMajor;
$\max(1, \mathbf{n} \times \mathbf{pdxres})$ when **order** = Nag_RowMajor.

The (i, j)th element of the matrix is stored in

xres$[(j-1) \times$ **pdxres** $+ i - 1]$ when **order** = Nag_ColMajor;
xres$[(i-1) \times$ **pdxres** $+ j - 1]$ when **order** = Nag_RowMajor.

On exit: the predictor variables' residual matrix X_k.

18: **pdxres** – Integer *Input*

On entry: the stride separating row or column elements (depending on the value of **order**) in the array **xres**.

Constraints:

if **order** = Nag_ColMajor, **pdxres** $\geq$ **n**;
if **order** = Nag_RowMajor, **pdxres** $\geq$ **ip**.

19: **yres**$[dim]$ – double *Output*

Note: the dimension, *dim*, of the array **yres** must be at least

$\max(1, \mathbf{pdyres} \times \mathbf{my})$ when **order** = Nag_ColMajor;
$\max(1, \mathbf{n} \times \mathbf{pdyres})$ when **order** = Nag_RowMajor.

The (i, j)th element of the matrix is stored in

yres$[(j-1) \times$ **pdyres** $+ i - 1]$ when **order** = Nag_ColMajor;
yres$[(i-1) \times$ **pdyres** $+ j - 1]$ when **order** = Nag_RowMajor.

On exit: the residuals for each response variable, Y_k.

20: **pdyres** – Integer *Input*

On entry: the stride separating row or column elements (depending on the value of **order**) in the array **yres**.

Constraints:

if **order** = Nag_ColMajor, **pdyres** $\geq$ **n**;
if **order** = Nag_RowMajor, **pdyres** $\geq$ **my**.

21: **w**$[dim]$ – double *Output*

Note: the dimension, *dim*, of the array **w** must be at least

$\max(1, \mathbf{pdw} \times \mathbf{maxfac})$ when **order** = Nag_ColMajor;
$\max(1, \mathbf{ip} \times \mathbf{pdw})$ when **order** = Nag_RowMajor.

The (i, j)th element of the matrix W is stored in

w$[(j-1) \times$ **pdw** $+ i - 1]$ when **order** = Nag_ColMajor;
w$[(i-1) \times$ **pdw** $+ j - 1]$ when **order** = Nag_RowMajor.

On exit: the jth column of W contains the x-weights w_j, for $j = 1, 2, \ldots,$ **maxfac**.

22: **pdw** – Integer *Input*

On entry: the stride separating row or column elements (depending on the value of **order**) in the array **w**.

Constraints:

if **order** = Nag_ColMajor, **pdw** $\geq$ **ip**;
if **order** = Nag_RowMajor, **pdw** $\geq$ **maxfac**.

23: **p**[dim] – double *Output*

Note: the dimension, *dim*, of the array **p** must be at least

max(1, **pdp** $\times$ **maxfac**) when **order** = Nag_ColMajor;
max(1, **ip** $\times$ **pdp**) when **order** = Nag_RowMajor.

The (i,j)th element of the matrix P is stored in

p[$(j-1) \times$ **pdp** $+ i - 1$] when **order** = Nag_ColMajor;
p[$(i-1) \times$ **pdp** $+ j - 1$] when **order** = Nag_RowMajor.

On exit: the jth column of P contains the x-loadings p_j, for $j = 1, 2, \ldots,$ **maxfac**.

24: **pdp** – Integer *Input*

On entry: the stride separating row or column elements (depending on the value of **order**) in the array **p**.

Constraints:

if **order** = Nag_ColMajor, **pdp** $\geq$ **ip**;
if **order** = Nag_RowMajor, **pdp** $\geq$ **maxfac**.

25: **t**[dim] – double *Output*

Note: the dimension, *dim*, of the array **t** must be at least

max(1, **pdt** $\times$ **maxfac**) when **order** = Nag_ColMajor;
max(1, **n** $\times$ **pdt**) when **order** = Nag_RowMajor.

The (i,j)th element of the matrix T is stored in

t[$(j-1) \times$ **pdt** $+ i - 1$] when **order** = Nag_ColMajor;
t[$(i-1) \times$ **pdt** $+ j - 1$] when **order** = Nag_RowMajor.

On exit: the jth column of T contains the x-scores t_j, for $j = 1, 2, \ldots,$ **maxfac**.

26: **pdt** – Integer *Input*

On entry: the stride separating row or column elements (depending on the value of **order**) in the array **t**.

Constraints:

if **order** = Nag_ColMajor, **pdt** $\geq$ **n**;
if **order** = Nag_RowMajor, **pdt** $\geq$ **maxfac**.

27: **c**[dim] – double *Output*

Note: the dimension, *dim*, of the array **c** must be at least

max(1, **pdc** $\times$ **maxfac**) when **order** = Nag_ColMajor;
max(1, **my** $\times$ **pdc**) when **order** = Nag_RowMajor.

The (i,j)th element of the matrix C is stored in

c[$(j-1) \times$ **pdc** $+ i - 1$] when **order** = Nag_ColMajor;
c[$(i-1) \times$ **pdc** $+ j - 1$] when **order** = Nag_RowMajor.

On exit: the jth column of C contains the y-loadings c_j, for $j = 1, 2, \ldots,$ **maxfac**.

28: **pdc** – Integer *Input*

On entry: the stride separating row or column elements (depending on the value of **order**) in the array **c**.

Constraints:

if **order** = Nag_ColMajor, **pdc** $\geq$ **my**;
if **order** = Nag_RowMajor, **pdc** $\geq$ **maxfac**.

29: **u**[dim] – double *Output*

Note: the dimension, *dim*, of the array **u** must be at least

$\max(1, \textbf{pdu} \times \textbf{maxfac})$ when **order** = Nag_ColMajor;
$\max(1, \textbf{n} \times \textbf{pdu})$ when **order** = Nag_RowMajor.

The (i, j)th element of the matrix U is stored in

u$[(j-1) \times$ **pdu** $+ i - 1]$ when **order** = Nag_ColMajor;
u$[(i-1) \times$ **pdu** $+ j - 1]$ when **order** = Nag_RowMajor.

On exit: the jth column of U contains the y-scores u_j, for $j = 1, 2, \ldots,$ **maxfac**.

30: **pdu** – Integer *Input*

On entry: the stride separating row or column elements (depending on the value of **order**) in the array **u**.

Constraints:

if **order** = Nag_ColMajor, **pdu** $\geq$ **n**;
if **order** = Nag_RowMajor, **pdu** $\geq$ **maxfac**.

31: **xcv**[**maxfac**] – double *Output*

On exit: **xcv**$[j-1]$ contains the cumulative percentage of variance in the predictor variables explained by the first j factors, for $j = 1, 2, \ldots,$ **maxfac**.

32: **ycv**[dim] – double *Output*

Note: the dimension, *dim*, of the array **ycv** must be at least

$\max(1, \textbf{pdycv} \times \textbf{my})$ when **order** = Nag_ColMajor;
$\max(1, \textbf{maxfac} \times \textbf{pdycv})$ when **order** = Nag_RowMajor.

Where **YCV**(i, j) appears in this document, it refers to the array element

ycv$[(j-1) \times$ **pdycv** $+ i - 1]$ when **order** = Nag_ColMajor;
ycv$[(i-1) \times$ **pdycv** $+ j - 1]$ when **order** = Nag_RowMajor.

On exit: **YCV**(i, j) is the cumulative percentage of variance of the jth response variable explained by the first i factors, for $i = 1, 2, \ldots,$ **maxfac** and $j = 1, 2, \ldots,$ **my**.

33: **pdycv** – Integer *Input*

On entry: the stride separating row or column elements (depending on the value of **order**) in the array **ycv**.

Constraints:

if **order** = Nag_ColMajor, **pdycv** $\geq$ **maxfac**;
if **order** = Nag_RowMajor, **pdycv** $\geq$ **my**.

34: **fail** – NagError * *Input/Output*

The NAG error argument (see Section 2.7 in How to Use the NAG Library and its Documentation).

6 Error Indicators and Warnings

NE_ALLOC_FAIL

Dynamic memory allocation failed.
See Section 2.3.1.2 in How to Use the NAG Library and its Documentation for further information.

NE_BAD_PARAM

On entry, argument ⟨*value*⟩ had an illegal value.

NE_INT

On entry, **mx** = ⟨*value*⟩.
Constraint: **mx** > 1.

On entry, **my** = ⟨*value*⟩.
Constraint: **my** ≥ 1.

On entry, **n** = ⟨*value*⟩.
Constraint: **n** > 1.

On entry, **pdc** = ⟨*value*⟩.
Constraint: **pdc** > 0.

On entry, **pdp** = ⟨*value*⟩.
Constraint: **pdp** > 0.

On entry, **pdt** = ⟨*value*⟩.
Constraint: **pdt** > 0.

On entry, **pdu** = ⟨*value*⟩.
Constraint: **pdu** > 0.

On entry, **pdw** = ⟨*value*⟩.
Constraint: **pdw** > 0.

On entry, **pdx** = ⟨*value*⟩.
Constraint: **pdx** > 0.

On entry, **pdxres** = ⟨*value*⟩.
Constraint: **pdxres** > 0.

On entry, **pdy** = ⟨*value*⟩.
Constraint: **pdy** > 0.

On entry, **pdycv** = ⟨*value*⟩.
Constraint: **pdycv** > 0.

On entry, **pdyres** = ⟨*value*⟩.
Constraint: **pdyres** > 0.

NE_INT_2

On entry, **ip** = ⟨*value*⟩ and **mx** = ⟨*value*⟩.
Constraint: $1 <$ **ip** $\leq$ **mx**.

On entry, **maxfac** = ⟨*value*⟩ and **ip** = ⟨*value*⟩.
Constraint: $1 \leq$ **maxfac** $\leq$ **ip**.

On entry, **pdc** = ⟨*value*⟩ and **maxfac** = ⟨*value*⟩.
Constraint: **pdc** ≥ **maxfac**.

On entry, **pdc** = ⟨*value*⟩ and **my** = ⟨*value*⟩.
Constraint: **pdc** ≥ **my**.

On entry, **pdp** = ⟨*value*⟩ and **ip** = ⟨*value*⟩.
Constraint: **pdp** ≥ **ip**.

On entry, **pdp** = ⟨*value*⟩ and **maxfac** = ⟨*value*⟩.
Constraint: **pdp** ≥ **maxfac**.

On entry, **pdt** = ⟨*value*⟩ and **maxfac** = ⟨*value*⟩.
Constraint: **pdt** ≥ **maxfac**.

On entry, **pdt** = ⟨*value*⟩ and **n** = ⟨*value*⟩.
Constraint: **pdt** ≥ **n**.

On entry, **pdu** = ⟨*value*⟩ and **maxfac** = ⟨*value*⟩.
Constraint: **pdu** ≥ **maxfac**.

On entry, **pdu** = ⟨*value*⟩ and **n** = ⟨*value*⟩.
Constraint: **pdu** ≥ **n**.

On entry, **pdw** = ⟨*value*⟩ and **ip** = ⟨*value*⟩.
Constraint: **pdw** ≥ **ip**.

On entry, **pdw** = ⟨*value*⟩ and **maxfac** = ⟨*value*⟩.
Constraint: **pdw** ≥ **maxfac**.

On entry, **pdx** = ⟨*value*⟩ and **mx** = ⟨*value*⟩.
Constraint: **pdx** ≥ **mx**.

On entry, **pdx** = ⟨*value*⟩ and **n** = ⟨*value*⟩.
Constraint: **pdx** ≥ **n**.

On entry, **pdxres** = ⟨*value*⟩ and **ip** = ⟨*value*⟩.
Constraint: **pdxres** ≥ **ip**.

On entry, **pdxres** = ⟨*value*⟩ and **n** = ⟨*value*⟩.
Constraint: **pdxres** ≥ **n**.

On entry, **pdy** = ⟨*value*⟩ and **my** = ⟨*value*⟩.
Constraint: **pdy** ≥ **my**.

On entry, **pdy** = ⟨*value*⟩ and **n** = ⟨*value*⟩.
Constraint: **pdy** ≥ **n**.

On entry, **pdycv** = ⟨*value*⟩ and **maxfac** = ⟨*value*⟩.
Constraint: **pdycv** ≥ **maxfac**.

On entry, **pdycv** = ⟨*value*⟩ and **my** = ⟨*value*⟩.
Constraint: **pdycv** ≥ **my**.

On entry, **pdyres** = ⟨*value*⟩ and **my** = ⟨*value*⟩.
Constraint: **pdyres** ≥ **my**.

On entry, **pdyres** = ⟨*value*⟩ and **n** = ⟨*value*⟩.
Constraint: **pdyres** ≥ **n**.

NE_INT_ARG_CONS

On entry, **ip** is not equal to the sum of **isx** elements: **ip** = ⟨*value*⟩, sum(**isx**) = ⟨*value*⟩.

NE_INT_ARRAY_VAL_1_OR_2

On entry, element ⟨*value*⟩ of **isx** is invalid.

NE_INTERNAL_ERROR

An internal error has occurred in this function. Check the function call and any array sizes. If the call is correct then please contact NAG for assistance.

An unexpected error has been triggered by this function. Please contact NAG.
See Section 2.7.6 in How to Use the NAG Library and its Documentation for further information.

NE_NO_LICENCE

Your licence key may have expired or may not have been installed correctly.
See Section 2.7.5 in How to Use the NAG Library and its Documentation for further information.

7 Accuracy

The computed singular value decomposition is nearly the exact singular value decomposition for a nearby matrix $(A + E)$, where

$$\|E\|_2 = O(\epsilon)\|A\|_2,$$

and ϵ is the ***machine precision***.

8 Parallelism and Performance

nag_pls_orth_scores_svd (g02lac) makes calls to BLAS and/or LAPACK routines, which may be threaded within the vendor library used by this implementation. Consult the documentation for the vendor library for further information.

Please consult the x06 Chapter Introduction for information on how to control and interrogate the OpenMP environment used within this function. Please also consult the Users' Note for your implementation for any additional implementation-specific information.

9 Further Comments

nag_pls_orth_scores_svd (g02lac) allocates internally $2mr + A + \max(3(A + B), 5A) + r$ elements of double storage, where $A = \min(m, r)$ and $B = \max(m, r)$.

10 Example

This example reads in data from an experiment to measure the biological activity in a chemical compound, and a PLS model is estimated.

10.1 Program Text

```
/* nag_pls_orth_scores_svd (g02lac) Example Program.
 *
 * NAGPRODCODE Version.
 *
 * Copyright 2016 Numerical Algorithms Group.
 *
 * Mark 26, 2016.
 */
/* Pre-processor includes */
#include <stdio.h>
#include <math.h>
#include <nag.h>
#include <nag_stdlib.h>
#include <nagg02.h>
#include <nagx04.h>

int main(void)
{
  /*Integer scalar and array declarations */
  Integer exit_status = 0;
```

```
  Integer i, ip, j, maxfac, mx, my, n;
  Integer pdc, pdp, pdt, pdu, pdw, pdx, pdxres, pdy, pdycv, pdyres;
  Integer *isx = 0;
  /*Double scalar and array declarations */
  double *c = 0, *p = 0, *t = 0, *u = 0, *w = 0, *x = 0, *xbar = 0;
  double *xcv = 0, *xres = 0, *xstd = 0, *y = 0, *ybar = 0;
  double *ycv = 0, *yres = 0, *ystd = 0;
  /*Character scalar and array declarations */
  char sscale[40];
  /*NAG Types */
  Nag_OrderType order;
  Nag_ScalePredictor scale;
  NagError fail;

  INIT_FAIL(fail);

  printf("nag_pls_orth_scores_svd (g02lac) Example Program Results\n");
  /* Skip header in data file. */
#ifdef _WIN32
  scanf_s("%*[^\n] ");
#else
  scanf("%*[^\n] ");
#endif
  /* Read data values. */
#ifdef _WIN32
  scanf_s("%" NAG_IFMT "%" NAG_IFMT "%" NAG_IFMT "%39s %" NAG_IFMT "%*[^\n] ",
          &n, &mx, &my, sscale, (unsigned)_countof(sscale), &maxfac);
#else
  scanf("%" NAG_IFMT "%" NAG_IFMT "%" NAG_IFMT "%39s %" NAG_IFMT "%*[^\n] ",
        &n, &mx, &my, sscale, &maxfac);
#endif
  scale = (Nag_ScalePredictor) nag_enum_name_to_value(sscale);

  if (!(isx = NAG_ALLOC(mx, Integer)))
  {
    printf("Allocation failure\n");
    exit_status = -1;
    goto END;
  }
  for (j = 0; j < mx; j++)
#ifdef _WIN32
    scanf_s("%" NAG_IFMT " ", &isx[j]);
#else
    scanf("%" NAG_IFMT " ", &isx[j]);
#endif
#ifdef _WIN32
  scanf_s("%*[^\n] ");
#else
  scanf("%*[^\n] ");
#endif
  ip = 0;
  for (j = 0; j < mx; j++) {
    if (isx[j] == 1)
      ip = ip + 1;
  }
#ifdef NAG_COLUMN_MAJOR
  pdc = my;
  pdp = ip;
  pdt = n;
  pdu = n;
  pdw = ip;
  pdx = n;
#define X(I, J)    x[(J-1)*pdx + I-1]
  pdxres = n;
  pdy = n;
#define Y(I, J)    y[(J-1)*pdy + I-1]
  pdycv = maxfac;
#define YCV(I, J)  ycv[(J-1)*pdycv + I-1]
  pdyres = n;
  order = Nag_ColMajor;
#else
```

```
  pdc = maxfac;
  pdp = maxfac;
  pdt = maxfac;
  pdu = maxfac;
  pdw = maxfac;
  pdx = mx;
#define X(I, J)    x[(I-1)*pdx + J-1]
  pdxres = ip;
  pdy = my;
#define Y(I, J)    y[(I-1)*pdy + J-1]
  pdycv = my;
#define YCV(I, J)  ycv[(I-1)*pdycv + J-1]
  pdyres = my;
  order = Nag_RowMajor;
#endif
  /* Assign parameter values to corresponding variables */
  if (!(c = NAG_ALLOC(pdc * (order == Nag_RowMajor ? my : maxfac), double)) ||
      !(p = NAG_ALLOC(pdp * (order == Nag_RowMajor ? ip : maxfac), double)) ||
      !(t = NAG_ALLOC(pdt * (order == Nag_RowMajor ? n : maxfac), double)) ||
      !(u = NAG_ALLOC(pdu * (order == Nag_RowMajor ? n : maxfac), double)) ||
      !(w = NAG_ALLOC(pdw * (order == Nag_RowMajor ? ip : maxfac), double)) ||
      !(x = NAG_ALLOC(pdx * (order == Nag_RowMajor ? n : mx), double)) ||
      !(xbar = NAG_ALLOC(ip, double)) ||
      !(xcv = NAG_ALLOC(maxfac, double)) ||
      !(xres = NAG_ALLOC(pdxres * (order == Nag_RowMajor ? n : ip), double))
      || !(xstd = NAG_ALLOC(ip, double))
      || !(y = NAG_ALLOC(pdy * (order == Nag_RowMajor ? n : my), double))
      || !(ybar = NAG_ALLOC(my, double))
      || !(ycv =
           NAG_ALLOC(pdycv * (order == Nag_RowMajor ? maxfac : my), double))
      || !(yres =
           NAG_ALLOC(pdyres * (order == Nag_RowMajor ? n : my), double))
      || !(ystd = NAG_ALLOC(my, double)))
  {
    printf("Allocation failure\n");
    exit_status = -1;
    goto END;
  }
  /* Read data values. */
  for (i = 1; i <= n; i++) {
    for (j = 1; j <= mx; j++)
#ifdef _WIN32
      scanf_s("%lf ", &X(i, j));
#else
      scanf("%lf ", &X(i, j));
#endif
    for (j = 1; j <= my; j++)
#ifdef _WIN32
      scanf_s("%lf ", &Y(i, j));
#else
      scanf("%lf ", &Y(i, j));
#endif
  }
#ifdef _WIN32
  scanf_s("%*[^\n] ");
#else
  scanf("%*[^\n] ");
#endif
  /* Fit a PLS model. */
  /*
   * nag_pls_orth_scores_svd (g02lac)
   * Partial least squares
   */
  nag_pls_orth_scores_svd(order, n, mx, x, pdx, isx, ip, my, y, pdy, xbar,
                          ybar, scale, xstd, ystd, maxfac, xres, pdxres,
                          yres, pdyres, w, pdw, p, pdp, t, pdt, c, pdc, u,
                          pdu, xcv, ycv, pdycv, &fail);
  if (fail.code != NE_NOERROR) {
    printf("Error from nag_pls_orth_scores_svd (g02lac).\n%s\n",
           fail.message);
    exit_status = 1;
```

```
    goto END;
  }
  /*
   * nag_gen_real_mat_print (x04cac)
   * Print real general matrix (easy-to-use)
   */
  fflush(stdout);
  nag_gen_real_mat_print(order, Nag_GeneralMatrix, Nag_NonUnitDiag, ip,
                         maxfac, p, pdp, "x-loadings, P", 0, &fail);
  if (fail.code != NE_NOERROR) {
    printf("Error from nag_gen_real_mat_print (x04cac).\n%s\n", fail.message);
    exit_status = 1;
    goto END;
  }
  /*
   * nag_gen_real_mat_print (x04cac)
   * Print real general matrix (easy-to-use)
   */
  fflush(stdout);
  nag_gen_real_mat_print(order, Nag_GeneralMatrix, Nag_NonUnitDiag, n,
                         maxfac, t, pdt, "x-scores, T", 0, &fail);
  if (fail.code != NE_NOERROR) {
    printf("Error from nag_gen_real_mat_print (x04cac).\n%s\n", fail.message);
    exit_status = 1;
    goto END;
  }
  /*
   * nag_gen_real_mat_print (x04cac)
   * Print real general matrix (easy-to-use)
   */
  fflush(stdout);
  nag_gen_real_mat_print(order, Nag_GeneralMatrix, Nag_NonUnitDiag, my,
                         maxfac, c, pdc, "y-loadings, C", 0, &fail);
  if (fail.code != NE_NOERROR) {
    printf("Error from nag_gen_real_mat_print (x04cac).\n%s\n", fail.message);
    exit_status = 1;
    goto END;
  }
  /*
   * nag_gen_real_mat_print (x04cac)
   * Print real general matrix (easy-to-use)
   */
  fflush(stdout);
  nag_gen_real_mat_print(order, Nag_GeneralMatrix, Nag_NonUnitDiag, n,
                         maxfac, u, pdu, "y-scores, U", 0, &fail);
  if (fail.code != NE_NOERROR) {
    printf("Error from nag_gen_real_mat_print (x04cac).\n%s\n", fail.message);
    exit_status = 1;
    goto END;
  }
  printf("\n");
  printf("%s\n", "Explained Variance");
  printf("%12s%24s\n", "Model effects", "Dependent variable(s)");
  for (i = 1; i <= maxfac; i++) {
    printf("%12.6f", xcv[i - 1]);
    for (j = 1; j <= my; j++)
      printf("%12.6f%s", YCV(i, j), j % 10 ? " " : "\n");
    printf("\n");
  }

END:
  NAG_FREE(c);
  NAG_FREE(p);
  NAG_FREE(t);
  NAG_FREE(u);
  NAG_FREE(w);
  NAG_FREE(x);
  NAG_FREE(xbar);
  NAG_FREE(xcv);
  NAG_FREE(xres);
  NAG_FREE(xstd);
```

```
  NAG_FREE(y);
  NAG_FREE(ybar);
  NAG_FREE(ycv);
  NAG_FREE(yres);
  NAG_FREE(ystd);
  NAG_FREE(isx);

  return exit_status;
}
```

10.2 Program Data

```
nag_pls_orth_scores_svd (g02lac) Example Program Data
15 15 1 Nag_PredStdScale 4 : n, mx, my, iscale, maxfac
1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 : isx
-2.6931 -2.5271 -1.2871  3.0777  0.3891 -0.0701  1.9607 -1.6324  0.5746
1.9607 -1.6324  0.574 2.8369  1.4092 -3.1398 0.00
-2.6931 -2.5271 -1.2871  3.0777  0.3891 -0.0701  1.9607 -1.6324  0.5746
0.0744 -1.7333  0.0902  2.8369  1.4092 -3.1398 0.28
-2.6931 -2.5271 -1.2871  3.0777  0.3891 -0.0701  0.0744 -1.7333  0.0902
1.9607 -1.6324  0.5746  2.8369  1.4092 -3.1398 0.20
-2.6931 -2.5271 -1.2871  3.0777  0.3891 -0.0701  0.0744 -1.7333  0.0902
0.0744 -1.7333  0.0902  2.8369  1.4092 -3.1398 0.51
-2.6931 -2.5271 -1.2871  2.8369  1.4092 -3.1398  0.0744 -1.7333  0.0902
0.0744 -1.7333  0.0902  2.8369  1.4092 -3.1398 0.11
-2.6931 -2.5271 -1.2871  3.0777  0.3891 -0.0701 -4.7548  3.6521  0.8524
0.0744 -1.7333  0.0902  2.8369  1.4092 -3.1398 2.73
-2.6931 -2.5271 -1.2871  3.0777  0.3891 -0.0701  0.0744 -1.7333  0.0902
0.0744 -1.7333  0.0902 -1.2201  0.8829  2.2253 0.18
-2.6931 -2.5271 -1.2871  3.0777  0.3891 -0.0701  2.4064  1.7438  1.1057
0.0744 -1.7333  0.0902  2.8369  1.4092 -3.1398 1.53
-2.6931 -2.5271 -1.2871  0.0744 -1.7333  0.0902  0.0744 -1.7333  0.0902
0.0744 -1.7333  0.0902  2.8369  1.4092 -3.1398 -0.10
 2.2261 -5.3648  0.3049  3.0777  0.3891 -0.0701  0.0744 -1.7333  0.0902
0.0744 -1.7333  0.0902  2.8369  1.4092 -3.1398 -0.52
-4.1921 -1.0285 -0.9801  3.0777  0.3891 -0.0701  0.0744 -1.7333  0.0902
0.0744 -1.7333  0.0902  2.8369  1.4092 -3.1398 0.40
-4.9217  1.2977  0.4473  3.0777  0.3891 -0.0701  0.0744 -1.7333  0.0902
0.0744 -1.7333  0.0902  2.8369  1.4092 -3.1398 0.30
-2.6931 -2.5271 -1.2871  3.0777  0.3891 -0.0701  2.2261 -5.3648  0.3049
2.2261 -5.3648  0.3049  2.8369  1.4092 -3.1398 -1.00
-2.6931 -2.5271 -1.2871  3.0777  0.3891 -0.0701 -4.9217  1.2977  0.4473
0.0744 -1.7333  0.0902  2.8369  1.4092 -3.1398 1.57
-2.6931 -2.5271 -1.2871  3.0777  0.3891 -0.0701 -4.1921 -1.0285 -0.9801
0.0744 -1.7333  0.0902  2.8369  1.4092 -3.1398 0.59 : End of observations
```

10.3 Program Results

```
nag_pls_orth_scores_svd (g02lac) Example Program Results
 x-loadings, P
             1          2          3          4
  1     -0.6708    -1.0047     0.6505     0.6169
  2      0.4943     0.1355    -0.9010    -0.2388
  3     -0.4167    -1.9983    -0.5538     0.8474
  4      0.3930     1.2441    -0.6967    -0.4336
  5      0.3267     0.5838    -1.4088    -0.6323
  6      0.0145     0.9607     1.6594     0.5361
  7     -2.4471     0.3532    -1.1321    -1.3554
  8      3.5198     0.6005     0.2191     0.0380
  9      1.0973     2.0635    -0.4074    -0.3522
 10     -2.4466     2.5640    -0.4806     0.3819
 11      2.2732    -1.3110    -0.7686    -1.8959
 12     -1.7987     2.4088    -0.9475    -0.4727
 13      0.3629     0.2241    -2.6332     2.3739
 14      0.3629     0.2241    -2.6332     2.3739
 15     -0.3629    -0.2241     2.6332    -2.3739
 x-scores, T
          1       2       3       4
  1  -0.1896  0.3898 -0.2502 -0.2479
  2   0.0201 -0.0013 -0.1726 -0.2042
```

```
  3  -0.1889  0.3141 -0.1727 -0.1350
  4   0.0210 -0.0773 -0.0950 -0.0912
  5  -0.0090 -0.2649 -0.4195 -0.1327
  6   0.5479  0.2843  0.1914  0.2727
  7  -0.0937 -0.0579  0.6799 -0.6129
  8   0.2500  0.2033 -0.1046 -0.1014
  9  -0.1005 -0.2992  0.2131  0.1223
 10  -0.1810 -0.4427  0.0559  0.2114
 11   0.0497 -0.0762 -0.1526 -0.0771
 12   0.0173 -0.2517 -0.2104  0.1044
 13  -0.6002  0.3596  0.1876  0.4812
 14   0.3796  0.1338  0.1410  0.1999
 15   0.0773 -0.2139  0.1085  0.2106
 y-loadings, C
           1          2          3          4
 1      3.5425     1.0475     0.2548     0.1866
 y-scores, U
            1          2          3          4
  1     -1.7670     0.1812    -0.0600    -0.0320
  2     -0.6724    -0.2735    -0.0662    -0.0402
  3     -0.9852     0.4097     0.0158     0.0198
  4      0.2267    -0.0107     0.0180     0.0177
  5     -1.3370    -0.3619    -0.0173     0.0073
  6      8.9056     0.6000     0.0701     0.0422
  7     -1.0634     0.0332     0.0235    -0.0151
  8      4.2143     0.3184     0.0232     0.0219
  9     -2.1580    -0.2652     0.0153     0.0011
 10     -3.7999    -0.4520     0.0082     0.0034
 11     -0.2033    -0.2446    -0.0392    -0.0214
 12     -0.5942    -0.2398     0.0089     0.0165
 13     -5.6764     0.5487     0.0375     0.0185
 14      4.3707    -0.1161    -0.0639    -0.0535
 15      0.5395    -0.1274     0.0261     0.0139

Explained Variance
Model effects   Dependent variable(s)
   16.902124   89.638060
   29.674338   97.476270
   44.332404   97.939839
   56.172041   98.188474
```