

NAG Library Function Document

nag_prob_chi_sq_vector (g01scc)

1 Purpose

nag_prob_chi_sq_vector (g01scc) returns a number of lower or upper tail probabilities for the χ^2 -distribution with real degrees of freedom.

2 Specification

```
#include <nag.h>
#include <nagg01.h>

void nag_prob_chi_sq_vector (Integer ltail,
    const Nag_TailProbability tail[], Integer lx, const double x[],
    Integer ldf, const double df[], double p[], Integer ivalid[],
    NagError *fail)
```

3 Description

The lower tail probability for the χ^2 -distribution with ν_i degrees of freedom, $P = (X_i \leq x_i : \nu_i)$ is defined by:

$$P = (X_i \leq x_i : \nu_i) = \frac{1}{2^{\nu_i/2} \Gamma(\nu_i/2)} \int_{0.0}^{x_i} X_i^{\nu_i/2-1} e^{-X_i/2} dX_i, \quad x_i \geq 0, \nu_i > 0.$$

To calculate $P = (X_i \leq x_i : \nu_i)$ a transformation of a gamma distribution is employed, i.e., a χ^2 -distribution with ν_i degrees of freedom is equal to a gamma distribution with scale parameter 2 and shape parameter $\nu_i/2$.

The input arrays to this function are designed to allow maximum flexibility in the supply of vector arguments by re-using elements of any arrays that are shorter than the total number of evaluations required. See Section 2.6 in the g01 Chapter Introduction for further information.

4 References

Abramowitz M and Stegun I A (1972) *Handbook of Mathematical Functions* (3rd Edition) Dover Publications

Hastings N A J and Peacock J B (1975) *Statistical Distributions* Butterworth

5 Arguments

- 1: **ltail** – Integer *Input*
On entry: the length of the array **tail**.
Constraint: **ltail** > 0.
- 2: **tail[ltail]** – const Nag_TailProbability *Input*
On entry: indicates whether the lower or upper tail probabilities are required. For $j = (i - 1) \bmod \mathbf{ltail}$, for $i = 1, 2, \dots, \max(\mathbf{ltail}, \mathbf{lx}, \mathbf{ldf})$:
tail[j] = Nag_LowerTail
The lower tail probability is returned, i.e., $p_i = P(X_i \leq x_i : \nu_i)$.

tail[*j*] = Nag_UpperTail

The upper tail probability is returned, i.e., $p_i = P(X_i \geq x_i : \nu_i)$.

Constraint: **tail**[*j* - 1] = Nag_LowerTail or Nag_UpperTail, for $j = 1, 2, \dots, \mathbf{ltail}$.

- 3: **lx** – Integer *Input*
On entry: the length of the array **x**.
Constraint: **lx** > 0.

- 4: **x**[**lx**] – const double *Input*
On entry: x_i , the values of the χ^2 variates with ν_i degrees of freedom with $x_i = \mathbf{x}[j]$, $j = (i - 1) \bmod \mathbf{lx}$.
Constraint: **x**[*j* - 1] ≥ 0.0, for $j = 1, 2, \dots, \mathbf{lx}$.

- 5: **ldf** – Integer *Input*
On entry: the length of the array **df**.
Constraint: **ldf** > 0.

- 6: **df**[**ldf**] – const double *Input*
On entry: ν_i , the degrees of freedom of the χ^2 -distribution with $\nu_i = \mathbf{df}[j]$, $j = (i - 1) \bmod \mathbf{ldf}$.
Constraint: **df**[*j* - 1] > 0.0, for $j = 1, 2, \dots, \mathbf{ldf}$.

- 7: **p**[*dim*] – double *Output*
Note: the dimension, *dim*, of the array **p** must be at least max(**ltail**, **ldf**, **lx**).
On exit: p_i , the probabilities for the χ^2 distribution.

- 8: **invalid**[*dim*] – Integer *Output*
Note: the dimension, *dim*, of the array **invalid** must be at least max(**ltail**, **ldf**, **lx**).
On exit: **invalid**[*i* - 1] indicates any errors with the input arguments, with
invalid[*i* - 1] = 0
 No error.
invalid[*i* - 1] = 1
 On entry, invalid value supplied in **tail** when calculating p_i .
invalid[*i* - 1] = 2
 On entry, $x_i < 0.0$.
invalid[*i* - 1] = 3
 On entry, $\nu_i \leq 0.0$.
invalid[*i* - 1] = 4
 The solution has failed to converge while calculating the gamma variate. The result returned should represent an approximation to the solution.

- 9: **fail** – NagError * *Input/Output*
 The NAG error argument (see Section 2.7 in How to Use the NAG Library and its Documentation).

6 Error Indicators and Warnings

NE_ALLOC_FAIL

Dynamic memory allocation failed.

See Section 2.3.1.2 in How to Use the NAG Library and its Documentation for further information.

NE_ARRAY_SIZE

On entry, array size = $\langle value \rangle$.

Constraint: **ldf** > 0.

On entry, array size = $\langle value \rangle$.

Constraint: **itail** > 0.

On entry, array size = $\langle value \rangle$.

Constraint: **ix** > 0.

NE_BAD_PARAM

On entry, argument $\langle value \rangle$ had an illegal value.

NE_INTERNAL_ERROR

An internal error has occurred in this function. Check the function call and any array sizes. If the call is correct then please contact NAG for assistance.

An unexpected error has been triggered by this function. Please contact NAG.

See Section 2.7.6 in How to Use the NAG Library and its Documentation for further information.

NE_NO_LICENCE

Your licence key may have expired or may not have been installed correctly.

See Section 2.7.5 in How to Use the NAG Library and its Documentation for further information.

NW_INVALID

On entry, at least one value of **x**, **df** or **tail** was invalid, or the solution failed to converge.

Check **invalid** for more information.

7 Accuracy

A relative accuracy of five significant figures is obtained in most cases.

8 Parallelism and Performance

nag_prob_chi_sq_vector (g01scc) is not threaded in any implementation.

9 Further Comments

For higher accuracy the transformation described in Section 3 may be used with a direct call to nag_incomplete_gamma (s14bac).

10 Example

Values from various χ^2 -distributions are read, the lower tail probabilities calculated, and all these values printed out.

10.1 Program Text

```

/* nag_prob_chi_sq_vector (g01scc) Example Program.
 *
 * NAGPRODCODE Version.
 *
 * Copyright 2016 Numerical Algorithms Group.
 *
 * Mark 26, 2016.
 */
#include <stdio.h>
#include <nag.h>
#include <nag_stdlib.h>
#include <nagg01.h>

int main(void)
{
    /* Integer scalar and array declarations */
    Integer ltail, lx, ldf, i, lout;
    Integer *ivalid = 0;
    Integer exit_status = 0;

    /* NAG structures */
    NagError fail;
    Nag_TailProbability *tail = 0;

    /* Double scalar and array declarations */
    double *x = 0, *df = 0, *p = 0;

    /* Character scalar and array declarations */
    char ctail[40];

    /* Initialize the error structure to print out any error messages */
    INIT_FAIL(fail);

    printf("nag_prob_chi_sq_vector (g01scc) Example Program Results\n\n");

    /* Skip heading in data file */
#ifdef _WIN32
    scanf_s("%*[\n] ");
#else
    scanf("%*[\n] ");
#endif

    /* Read in the input vectors */
#ifdef _WIN32
    scanf_s("%" NAG_IFMT "%*[\n] ", &ltail);
#else
    scanf("%" NAG_IFMT "%*[\n] ", &ltail);
#endif
    if (!(tail = NAG_ALLOC(ltail, Nag_TailProbability))) {
        printf("Allocation failure\n");
        exit_status = -1;
        goto END;
    }
    for (i = 0; i < ltail; i++) {
#ifdef _WIN32
        scanf_s("%39s", ctail, (unsigned)_countof(ctail));
#else
        scanf("%39s", ctail);
#endif
        tail[i] = (Nag_TailProbability) nag_enum_name_to_value(ctail);
    }
#ifdef _WIN32
    scanf_s("%*[\n] ");
#else
    scanf("%*[\n] ");
#endif

#ifdef _WIN32
    scanf_s("%" NAG_IFMT "%*[\n] ", &lx);

```

```

#else
    scanf("%" NAG_IFMT "%*[\n] ", &lx);
#endif
    if (!(x = NAG_ALLOC(lx, double)))
    {
        printf("Allocation failure\n");
        exit_status = -1;
        goto END;
    }
    for (i = 0; i < lx; i++)
#ifdef _WIN32
        scanf_s("%lf", &x[i]);
#else
        scanf("%lf", &x[i]);
#endif
#ifdef _WIN32
    scanf_s("%*[\n] ");
#else
    scanf("%*[\n] ");
#endif

#ifdef _WIN32
    scanf_s("%" NAG_IFMT "%*[\n] ", &ldf);
#else
    scanf("%" NAG_IFMT "%*[\n] ", &ldf);
#endif
    if (!(df = NAG_ALLOC(ldf, double)))
    {
        printf("Allocation failure\n");
        exit_status = -1;
        goto END;
    }
    for (i = 0; i < ldf; i++)
#ifdef _WIN32
        scanf_s("%lf", &df[i]);
#else
        scanf("%lf", &df[i]);
#endif
#ifdef _WIN32
    scanf_s("%*[\n] ");
#else
    scanf("%*[\n] ");
#endif

    /* Allocate memory for output */
    lout = MAX(ltail, MAX(lx, ldf));
    if (!(p = NAG_ALLOC(lout, double)) || !(ivalid = NAG_ALLOC(lout, Integer)))
    {
        printf("Allocation failure\n");
        exit_status = -1;
        goto END;
    }

    /* Calculate probability */
    nag_prob_chi_sq_vector(ltail, tail, lx, x, ldf, df, p, ivalid, &fail);
    if (fail.code != NE_NOERROR) {
        printf("Error from nag_prob_chi_sq_vector (g01scc).\n%s\n", fail.message);
        exit_status = 1;
        if (fail.code != NW_INVALID)
            goto END;
    }

    /* Display title */
    printf("          tail          x          df          p          ivalid\n");
    printf("-----\n");

    /* Display results */
    for (i = 0; i < lout; i++)
        printf(" %15s %6.3f %6.1f %6.4f %3" NAG_IFMT "\n",
            nag_enum_value_to_name(tail[i % ltail]), x[i % lx], df[i % ldf],
            p[i], ivalid[i]);

```

```

END:
    NAG_FREE(tail);
    NAG_FREE(x);
    NAG_FREE(df);
    NAG_FREE(p);
    NAG_FREE(ivalid);

    return (exit_status);
}

```

10.2 Program Data

nag_prob_chi_sq_vector (g01scc) Example Program Data

1		:: ltail
Nag_LowerTail		:: tail
3		:: lx
8.26 6.2 55.76		:: x
3		:: ldf
20.0 7.5 45.0		:: df

10.3 Program Results

nag_prob_chi_sq_vector (g01scc) Example Program Results

tail	x	df	p	ivalid
Nag_LowerTail	8.260	20.0	0.0100	0
Nag_LowerTail	6.200	7.5	0.4279	0
Nag_LowerTail	55.760	45.0	0.8694	0
