

NAG Library Function Document

nag_dtfsm (f16ylc)

1 Purpose

nag_dtfsm (f16ylc) performs one of the matrix-matrix operations

$$\begin{aligned} B &\leftarrow \alpha A^{-1}B, & B &\leftarrow \alpha A^{-T}B, \\ B &\leftarrow \alpha BA^{-1} & \text{or} & B &\leftarrow \alpha BA^{-T}, \end{aligned}$$

where A is a real triangular matrix stored in Rectangular Full Packed (RFP) format, B is an m by n real matrix, and α is a real scalar. A^{-T} denotes $(A^T)^{-1}$ or equivalently $(A^{-1})^T$.

No test for singularity or near-singularity of A is included in this function. Such tests must be performed before calling this function.

2 Specification

```
#include <nag.h>
#include <nagf16.h>

void nag_dtfsm (Nag_OrderType order, Nag_RFP_Store transr,
               Nag_SideType side, Nag_UploType uplo, Nag_TransType trans,
               Nag_DiagType diag, Integer m, Integer n, double alpha,
               const double ar[], double b[], Integer pdb, NagError *fail)
```

3 Description

nag_dtfsm (f16ylc) solves (for X) a triangular linear system of one of the forms

$$\begin{aligned} AX &= \alpha B, & A^T X &= \alpha B, \\ XA &= \alpha B & \text{or} & XA^T &= \alpha B, \end{aligned}$$

where A is a real triangular matrix stored in RFP format, B , X are m by n real matrices, and α is a real scalar. The RFP storage format is described in Section 3.3.3 in the f07 Chapter Introduction.

4 References

Gustavson F G, Waśniewski J, Dongarra J J and Langou J (2010) Rectangular full packed format for Cholesky's algorithm: factorization, solution, and inversion *ACM Trans. Math. Software* **37**, 2

5 Arguments

- 1: **order** – Nag_OrderType *Input*
On entry: the **order** argument specifies the two-dimensional storage scheme being used, i.e., row-major ordering or column-major ordering. C language defined storage is specified by **order** = Nag_RowMajor. See Section 2.3.1.3 in How to Use the NAG Library and its Documentation for a more detailed explanation of the use of this argument.
Constraint: **order** = Nag_RowMajor or Nag_ColMajor.
- 2: **transr** – Nag_RFP_Store *Input*
On entry: specifies whether the RFP representation of A is normal or transposed.
transr = Nag_RFP_Normal
The matrix A is stored in normal RFP format.

transr = Nag_RFP_Trans

The matrix A is stored in transposed RFP format.

Constraint: **transr** = Nag_RFP_Normal or Nag_RFP_Trans.

3: **side** – Nag_SideType

Input

On entry: specifies whether B is operated on from the left or the right, or similarly whether A (or its transpose) appears to the left or right of the solution matrix in the linear system to be solved.

side = Nag_LeftSide

B is pre-multiplied from the left. The system to be solved has the form $AX = \alpha B$ or $A^T X = \alpha B$.

side = Nag_RightSide

B is post-multiplied from the right. The system to be solved has the form $XA = \alpha B$ or $XA^T = \alpha B$.

Constraint: **side** = Nag_LeftSide or Nag_RightSide.

4: **uplo** – Nag_UploType

Input

On entry: specifies whether A is upper or lower triangular.

uplo = Nag_Upper

A is upper triangular.

uplo = Nag_Lower

A is lower triangular.

Constraint: **uplo** = Nag_Upper or Nag_Lower.

5: **trans** – Nag_TransType

Input

On entry: specifies whether the operation involves A^{-1} or A^{-T} , i.e., whether or not A is transposed in the linear system to be solved.

trans = Nag_NoTrans

The operation involves A^{-1} , i.e., A is not transposed.

trans = Nag_Trans

The operation involves A^{-T} , i.e., A is transposed.

Constraint: **trans** = Nag_NoTrans or Nag_Trans.

6: **diag** – Nag_DiagType

Input

On entry: specifies whether A has nonunit or unit diagonal elements.

diag = Nag_NonUnitDiag

The diagonal elements of A are stored explicitly.

diag = Nag_UnitDiag

The diagonal elements of A are assumed to be 1, the corresponding elements of **ar** are not referenced.

Constraint: **diag** = Nag_NonUnitDiag or Nag_UnitDiag.

7: **m** – Integer

Input

On entry: m , the number of rows of the matrix B .

Constraint: **m** ≥ 0 .

- 8: **n** – Integer *Input*
On entry: n , the number of columns of the matrix B .
Constraint: $n \geq 0$.
- 9: **alpha** – double *Input*
On entry: the scalar α .
- 10: **ar**[dim] – const double *Input*
Note: the dimension, dim , of the array **ar** must be at least
 $\max(1, m \times (m + 1)/2)$ when **side** = Nag_LeftSide;
 $\max(1, n \times (n + 1)/2)$ when **side** = Nag_RightSide.
On entry: the m by m triangular matrix A if **side** = Nag_LeftSide or the n by n triangular matrix A if **side** = Nag_RightSide, stored in RFP format (as specified by **transr**). The storage format is described in detail in Section 3.3.3 in the f07 Chapter Introduction. If **alpha** = 0.0, **ar** is not referenced.
- 11: **b**[dim] – double *Input/Output*
Note: the dimension, dim , of the array **b** must be at least
 $\max(1, pdb \times n)$ when **order** = Nag_ColMajor;
 $\max(1, m \times pdb)$ when **order** = Nag_RowMajor.
On entry: the m by n matrix B .
If **alpha** = 0, **b** need not be set.
On exit: the updated matrix B , or similarly the solution matrix X .
If **order** = Nag_ColMajor, B_{ij} is stored in **b**[($j - 1$) \times **pdb** + $i - 1$].
If **order** = Nag_RowMajor, B_{ij} is stored in **b**[($i - 1$) \times **pdb** + $j - 1$].
- 12: **pdb** – Integer *Input*
On entry: the stride separating row or column elements (depending on the value of **order**) in the array **b**.
Constraints:
if **order** = Nag_ColMajor, **pdb** $\geq \max(1, m)$;
if **order** = Nag_RowMajor, **pdb** $\geq \max(1, n)$.
- 13: **fail** – NagError * *Input/Output*
The NAG error argument (see Section 2.7 in How to Use the NAG Library and its Documentation).

6 Error Indicators and Warnings

NE_ALLOC_FAIL

Dynamic memory allocation failed.

See Section 2.3.1.2 in How to Use the NAG Library and its Documentation for further information.

NE_BAD_PARAM

On entry, argument $\langle value \rangle$ had an illegal value.

NE_INT

On entry, **m** = $\langle value \rangle$.

Constraint: **m** ≥ 0 .

On entry, **n** = $\langle value \rangle$.

Constraint: **n** ≥ 0 .

NE_INT_2

On entry, **pdb** = $\langle value \rangle$, **m** = $\langle value \rangle$.

Constraint: **pdb** $\geq \max(1, \mathbf{m})$.

On entry, **pdb** = $\langle value \rangle$ and **n** = $\langle value \rangle$.

Constraint: **pdb** $\geq \max(1, \mathbf{n})$.

NE_INTERNAL_ERROR

An internal error has occurred in this function. Check the function call and any array sizes. If the call is correct then please contact NAG for assistance.

An unexpected error has been triggered by this function. Please contact NAG.

See Section 2.7.6 in How to Use the NAG Library and its Documentation for further information.

NE_NO_LICENCE

Your licence key may have expired or may not have been installed correctly.

See Section 2.7.5 in How to Use the NAG Library and its Documentation for further information.

7 Accuracy

Not applicable.

8 Parallelism and Performance

nag_dtfsm (f16ylc) makes calls to BLAS and/or LAPACK routines, which may be threaded within the vendor library used by this implementation. Consult the documentation for the vendor library for further information.

Please consult the x06 Chapter Introduction for information on how to control and interrogate the OpenMP environment used within this function. Please also consult the Users' Note for your implementation for any additional implementation-specific information.

9 Further Comments

None.

10 Example

This example reads in the lower triangular part of a symmetric matrix A which it converts to RFP format. It also reads in α and a 6 by 4 matrix B and then performs the matrix-matrix operation $B \leftarrow \alpha A^{-1} B$.

10.1 Program Text

```
/* nag_dtfsm (f16ylc) Example Program.
 *
 * NAGPRODCODE Version.
 *
 * Copyright 2016 Numerical Algorithms Group.
 *
 * Mark 26, 2016.
 */
```

```

#include <nag.h>
#include <nag_stdlib.h>
#include <nagf01.h>
#include <nagf16.h>
#include <nagx04.h>

int main(void)
{
    /* Scalars */
    Integer exit_status = 0;
    double alpha;
    Integer i, j, m, n, pda, pdb;
    /* Arrays */
    double *a = 0, *ar = 0, *b = 0;
    char nag_enum_arg[40];
    /* Nag Types */
    Nag_OrderType order;
    Nag_RFP_Store transr;
    Nag_SideType side;
    Nag_UploType uplo;
    Nag_TransType trans;
    NagError fail;

    INIT_FAIL(fail);

    printf("nag_dtfs (f16ylc) Example Program Results\n");
    /* Skip heading in data file */
#ifdef _WIN32
    scanf_s("%*[\n] ");
#else
    scanf("%*[\n] ");
#endif
#ifdef _WIN32
    scanf_s("%" NAG_IFMT "%" NAG_IFMT "%*[\n] ", &m, &n);
#else
    scanf("%" NAG_IFMT "%" NAG_IFMT "%*[\n] ", &m, &n);
#endif
    pda = m;

#ifdef NAG_COLUMN_MAJOR
    order = Nag_ColMajor;
    pdb = m;
#define A(I, J) a[(J-1)*pda + I-1]
#define B(I, J) b[(J-1)*pdb + I-1]
#else
    order = Nag_RowMajor;
    pdb = n;
#define A(I, J) a[(I-1)*pda + J-1]
#define B(I, J) b[(I-1)*pdb + J-1]
#endif

    if (!(a = NAG_ALLOC(pda * m, double)) ||
        !(ar = NAG_ALLOC((m * (m + 1)) / 2, double)) ||
        !(b = NAG_ALLOC(m * n, double)))
    {
        printf("Allocation failure\n");
        exit_status = -1;
        goto END;
    }

    /* Nag_RFP_Store */
#ifdef _WIN32
    scanf_s("%39s ", nag_enum_arg, (unsigned)_countof(nag_enum_arg));
#else
    scanf("%39s ", nag_enum_arg);
#endif
    transr = (Nag_RFP_Store) nag_enum_name_to_value(nag_enum_arg);
    /* Nag_SideType */
#ifdef _WIN32
    scanf_s("%39s  %*[\n] ", nag_enum_arg, (unsigned)_countof(nag_enum_arg));

```

```

#else
    scanf("%39s  %*[\n] ", nag_enum_arg);
#endif
    side = (Nag_SideType) nag_enum_name_to_value(nag_enum_arg);
    /* Nag_UploType */
#ifdef _WIN32
    scanf_s("%39s ", nag_enum_arg, (unsigned)_countof(nag_enum_arg));
#else
    scanf("%39s ", nag_enum_arg);
#endif
    uplo = (Nag_UploType) nag_enum_name_to_value(nag_enum_arg);
    /* Nag_TransType */
#ifdef _WIN32
    scanf_s("%39s  %*[\n] ", nag_enum_arg, (unsigned)_countof(nag_enum_arg));
#else
    scanf("%39s  %*[\n] ", nag_enum_arg);
#endif
    trans = (Nag_TransType) nag_enum_name_to_value(nag_enum_arg);
#ifdef _WIN32
    scanf_s("%lf%*[\n] ", &alpha);
#else
    scanf("%lf%*[\n] ", &alpha);
#endif
    /* Read upper or lower triangle of matrix A from data file */
    if (uplo == Nag_Lower) {
        for (i = 1; i <= m; i++) {
            for (j = 1; j <= i; j++) {
#ifdef _WIN32
                scanf_s("%lf", &A(i, j));
#else
                scanf("%lf", &A(i, j));
#endif
            }
        }
    }
    else {
        for (i = 1; i <= m; i++) {
            for (j = i; j <= m; j++) {
#ifdef _WIN32
                scanf_s("%lf", &A(i, j));
#else
                scanf("%lf", &A(i, j));
#endif
            }
        }
    }
#ifdef _WIN32
    scanf_s("%*[\n] ");
#else
    scanf("%*[\n] ");
#endif

    /* Read matrix B from data file */
    for (i = 1; i <= m; i++) {
        for (j = 1; j <= n; j++) {
#ifdef _WIN32
            scanf_s("%lf", &B(i, j));
#else
            scanf("%lf", &B(i, j));
#endif
        }
    }
    /* Convert real triangular matrix A from full to rectangular full packed
     * storage format (stored in ar) using nag_dtrttf (f01vec).
     */
    nag_dtrttf(order, transr, uplo, m, a, pda, ar, &fail);
    if (fail.code != NE_NOERROR) {
        printf("Error from nag_dtrttf (f01vec).\n%s\n", fail.message);
        exit_status = 1;
        goto END;
    }
}

```

```

printf("\n");
/* Solve AX = B, where real triangular matrix A is stored using RFP format
 * in ar, using nag_dtfsm (f16ylc).
 */
nag_dtfsm(order, transr, side, uplo, trans, Nag_NonUnitDiag, m, n, alpha,
          ar, b, pdb, &fail);
if (fail.code != NE_NOERROR) {
    printf("Error from nag_dtfsm (f16ylc).\n%s\n", fail.message);
    exit_status = 1;
    goto END;
}

/* Print the result using easy-to-use real general matrix printing routine
 * nag_gen_real_mat_print (x04cac).
 */
fflush(stdout);
nag_gen_real_mat_print(order, Nag_GeneralMatrix, Nag_NonUnitDiag, m, n, b,
                      pdb, "The Solution", 0, &fail);
if (fail.code != NE_NOERROR) {
    printf("Error from nag_gen_real_mat_print (x04cac).\n%s\n", fail.message);
    exit_status = 1;
}

END:
    NAG_FREE(a);
    NAG_FREE(ar);
    NAG_FREE(b);
    return exit_status;
}

```

10.2 Program Data

nag_dtfsm (f16ylc) Example Program Data

```

6 4                      : m, n
Nag_RFP_Normal Nag_LeftSide : transr, side
Nag_Lower      Nag_NoTrans  : uplo, trans
4.21           : alpha

1.0
2.0  2.0
3.0  3.0  3.0
4.0  4.0  4.0  4.0
5.0  5.0  5.0  5.0  5.0
6.0  6.0  6.0  6.0  6.0  6.0 : matrix A

3.22  1.37  2.31  0.29
1.64  1.80  0.38 -1.52
1.87  2.87  2.02 -0.80
5.20 -2.99 -0.91 -3.87
1.83 -2.71 -2.81 -1.13
-1.10 -0.63 -0.50  0.81 : matrix B

```

10.3 Program Results

nag_dtfsm (f16ylc) Example Program Results

The Solution				
	1	2	3	4
1	13.5562	5.7677	9.7251	1.2209
2	-10.1040	-1.9787	-8.9252	-4.4205
3	-0.8280	0.2386	2.0348	2.0769
4	2.8488	-7.1745	-3.7925	-2.9505
5	-3.9321	0.8652	-1.4082	3.1217
6	-2.3127	1.8398	2.0152	1.5198
