

NAG Library Function Document

nag_dgb_norm (f16rbc)

1 Purpose

nag_dgb_norm (f16rbc) calculates the value of the 1-norm, the ∞ -norm, the Frobenius norm or the maximum absolute value of the elements of a real m by n band matrix stored in banded form.

2 Specification

```
#include <nag.h>
#include <nagf16.h>

void nag_dgb_norm (Nag_OrderType order, Nag_NormType norm, Integer m,
                  Integer n, Integer kl, Integer ku, const double ab[], Integer pdab,
                  double *r, NagError *fail)
```

3 Description

Given a real m by n banded matrix, A , nag_dgb_norm (f16rbc) calculates one of the values given by

$$\begin{aligned} \|A\|_1 &= \max_j \sum_{i=1}^m |a_{ij}| && \text{(the 1-norm of } A), \\ \|A\|_\infty &= \max_i \sum_{j=1}^n |a_{ij}| && \text{(the } \infty\text{-norm of } A), \\ \|A\|_F &= \left(\sum_{i=1}^m \sum_{j=1}^n |a_{ij}|^2 \right)^{1/2} && \text{(the Frobenius norm of } A), \quad \text{or} \\ &\max_{i,j} |a_{ij}| && \text{(the maximum absolute element value of } A). \end{aligned}$$

4 References

Basic Linear Algebra Subprograms Technical (BLAST) Forum (2001) *Basic Linear Algebra Subprograms Technical (BLAST) Forum Standard* University of Tennessee, Knoxville, Tennessee <http://www.netlib.org/blas/blast-forum/blas-report.pdf>

5 Arguments

- 1: **order** – Nag_OrderType *Input*
On entry: the **order** argument specifies the two-dimensional storage scheme being used, i.e., row-major ordering or column-major ordering. C language defined storage is specified by **order** = Nag_RowMajor. See Section 2.3.1.3 in How to Use the NAG Library and its Documentation for a more detailed explanation of the use of this argument.
Constraint: **order** = Nag_RowMajor or Nag_ColMajor.
- 2: **norm** – Nag_NormType *Input*
On entry: specifies the value to be returned.
norm = Nag_OneNorm
The 1-norm.

norm = Nag_FrobeniusNorm
The Frobenius (or Euclidean) norm.

norm = Nag_InfNorm
The ∞ -norm.

norm = Nag_MaxNorm
The value $\max_{i,j} |a_{ij}|$ (not a norm).

Constraint: **norm** = Nag_OneNorm, Nag_FrobeniusNorm, Nag_InfNorm or Nag_MaxNorm.

3: **m** – Integer *Input*

On entry: m , the number of rows of the matrix A .

Constraint: **m** ≥ 0 .

4: **n** – Integer *Input*

On entry: n , the number of columns of the matrix A .

Constraint: **n** ≥ 0 .

5: **kl** – Integer *Input*

On entry: k_l , the number of subdiagonals within the band of A .

Constraint: **kl** ≥ 0 .

6: **ku** – Integer *Input*

On entry: k_u , the number of superdiagonals within the band of A .

Constraint: **ku** ≥ 0 .

7: **ab**[*dim*] – const double *Input*

Note: the dimension, *dim*, of the array **ab** must be at least

$\max(1, \mathbf{pdab} \times \mathbf{n})$ when **order** = Nag_ColMajor;
 $\max(1, \mathbf{m} \times \mathbf{pdab})$ when **order** = Nag_RowMajor.

On entry: the m by n band matrix A .

This is stored as a notional two-dimensional array with row elements or column elements stored contiguously. The storage of elements A_{ij} , for row $i = 1, \dots, m$ and column $j = \max(1, i - k_l), \dots, \min(n, i + k_u)$, depends on the **order** argument as follows:

if **order** = Nag_ColMajor, A_{ij} is stored as **ab**[($j - 1$) \times **pdab** + **ku** + $i - j$];

if **order** = Nag_RowMajor, A_{ij} is stored as **ab**[($i - 1$) \times **pdab** + **kl** + $j - i$].

8: **pdab** – Integer *Input*

On entry: the stride separating row or column elements (depending on the value of **order**) of the matrix A in the array **ab**.

Constraint: **pdab** $\geq \mathbf{kl} + \mathbf{ku} + 1$.

9: **r** – double * *Output*

On exit: the value of the norm specified by **norm**.

10: **fail** – NagError * *Input/Output*

The NAG error argument (see Section 2.7 in How to Use the NAG Library and its Documentation).

6 Error Indicators and Warnings

NE_ALLOC_FAIL

Dynamic memory allocation failed.

See Section 2.3.1.2 in How to Use the NAG Library and its Documentation for further information.

NE_BAD_PARAM

On entry, argument $\langle value \rangle$ had an illegal value.

NE_INT

On entry, $\mathbf{kl} = \langle value \rangle$.

Constraint: $\mathbf{kl} \geq 0$.

On entry, $\mathbf{ku} = \langle value \rangle$.

Constraint: $\mathbf{ku} \geq 0$.

On entry, $\mathbf{m} = \langle value \rangle$.

Constraint: $\mathbf{m} \geq 0$.

On entry, $\mathbf{n} = \langle value \rangle$.

Constraint: $\mathbf{n} \geq 0$.

NE_INT_3

On entry, $\mathbf{pdab} = \langle value \rangle$, $\mathbf{kl} = \langle value \rangle$, $\mathbf{ku} = \langle value \rangle$.

Constraint: $\mathbf{pdab} \geq \mathbf{kl} + \mathbf{ku} + 1$.

NE_INTERNAL_ERROR

An unexpected error has been triggered by this function. Please contact NAG.

See Section 2.7.6 in How to Use the NAG Library and its Documentation for further information.

NE_NO_LICENCE

Your licence key may have expired or may not have been installed correctly.

See Section 2.7.5 in How to Use the NAG Library and its Documentation for further information.

7 Accuracy

The BLAS standard requires accurate implementations which avoid unnecessary over/underflow (see Section 2.7 of Basic Linear Algebra Subprograms Technical (BLAST) Forum (2001)).

8 Parallelism and Performance

`nag_dgb_norm` (f16rbc) is not threaded in any implementation.

9 Further Comments

None.

10 Example

Calculates the various norms of a 6 by 4 banded matrix with two subdiagonals and one superdiagonal.

10.1 Program Text

```

/* nag_dgb_norm (f16rbc) Example Program.
 *
 * NAGPRODCODE Version.
 *
 * Copyright 2016 Numerical Algorithms Group.
 *
 * Mark 26, 2016.
 */

#include <stdio.h>
#include <nag.h>
#include <nag_stdlib.h>
#include <nagf16.h>

int main(void)
{
    /* Scalars */
    double r_one, r_inf, r_f, r_max;
    Integer ab_size, exit_status, i, j, kl, ku;
    Integer m, n, pdab;

    /* Arrays */
    double *ab = 0;

    /* Nag Types */
    NagError fail;
    Nag_OrderType order;

#ifdef NAG_COLUMN_MAJOR
#define AB(I, J) ab[(J-1)*pdab + ku + I - J]
    order = Nag_ColMajor;
#else
#define AB(I, J) ab[(I-1)*pdab + kl + J - I]
    order = Nag_RowMajor;
#endif

    exit_status = 0;
    INIT_FAIL(fail);

    printf("nag_dgb_norm (f16rbc) Example Program Results\n\n");

    /* Skip heading in data file */
#ifdef _WIN32
    scanf_s("%*[\n] ");
#else
    scanf("%*[\n] ");
#endif

    /* Read the problem dimensions */
#ifdef _WIN32
    scanf_s("%" NAG_IFMT "%" NAG_IFMT "%" NAG_IFMT "%" NAG_IFMT "%*[\n] ",
            &m, &n, &kl, &ku);
#else
    scanf("%" NAG_IFMT "%" NAG_IFMT "%" NAG_IFMT "%" NAG_IFMT "%*[\n] ",
            &m, &n, &kl, &ku);
#endif

    pdab = kl + ku + 1;
#ifdef NAG_COLUMN_MAJOR
    ab_size = pdab * n;
#else
    ab_size = pdab * m;
#endif

    if (m > 0 && n > 0) {
        /* Allocate memory */
        if (!(ab = NAG_ALLOC(ab_size, double)))
        {

```

```

        printf("Allocation failure\n");
        exit_status = -1;
        goto END;
    }
}
else {
    printf("Invalid m or n\n");
    exit_status = 1;
    return exit_status;
}

/* Input matrix A. */

for (i = 1; i <= m; ++i) {
    for (j = MAX(1, i - kl); j <= MIN(n, i + ku); ++j)
#ifdef _WIN32
        scanf_s("%lf", &AB(i, j));
#else
        scanf("%lf", &AB(i, j));
#endif
#ifdef _WIN32
        scanf_s("%*[\n] ");
#else
        scanf("%*[\n] ");
#endif
}

/* nag_dgb_norm (f16rbc).
 * calculates norm of real valued general band matrix.
 */
nag_dgb_norm(order, Nag_OneNorm, m, n, kl, ku, ab, pdab, &r_one, &fail);

if (fail.code != NE_NOERROR)
    goto GB_FAIL;

nag_dgb_norm(order, Nag_InfNorm, m, n, kl, ku, ab, pdab, &r_inf, &fail);

if (fail.code != NE_NOERROR)
    goto GB_FAIL;

nag_dgb_norm(order, Nag_FrobeniusNorm, m, n, kl, ku, ab, pdab, &r_f, &fail);

if (fail.code != NE_NOERROR)
    goto GB_FAIL;

nag_dgb_norm(order, Nag_MaxNorm, m, n, kl, ku, ab, pdab, &r_max, &fail);

if (fail.code != NE_NOERROR)
    goto GB_FAIL;

/* Print norms of A. */
printf(" Norms of banded matrix A:\n\n");
printf(" One norm          = %7.4f\n", r_one);
printf(" Infinity norm     = %7.4f\n", r_inf);
printf(" Frobenius norm      = %7.4f\n", r_f);
printf(" Maximum norm       = %7.4f\n", r_max);
goto END;

GB_FAIL:
printf("Error from nag_dgb_norm.\n%s\n", fail.message);
exit_status = 1;

END:
    NAG_FREE(ab);

    return exit_status;
}

```

10.2 Program Data

```
nag_dgb_norm (f16rbc) Example Program Data
  6 4 2 1      :Values of m, n, kl, ku
    1.0  1.0
    2.0  2.0  2.0
    3.0  3.0  3.0  3.0
      4.0  4.0  4.0
        5.0  5.0
          6.0 : the end of matrix A
```

10.3 Program Results

```
nag_dgb_norm (f16rbc) Example Program Results
```

Norms of banded matrix A:

```
One norm      = 18.0000
Infinity norm = 12.0000
Frobenius norm = 13.5647
Maximum norm  =  6.0000
```
