

# NAG Library Function Document

## nag\_dtbsv (f16pkc)

### 1 Purpose

nag\_dtbsv (f16pkc) solves a system of equations given as a real triangular band matrix.

### 2 Specification

```
#include <nag.h>
#include <nagf16.h>

void nag_dtbsv (Nag_OrderType order, Nag_UploType uplo, Nag_TransType trans,
               Nag_DiagType diag, Integer n, Integer k, double alpha,
               const double ab[], Integer pdab, double x[], Integer incx,
               NagError *fail)
```

### 3 Description

nag\_dtbsv (f16pkc) performs one of the matrix-vector operations

$$x \leftarrow \alpha A^{-1}x \quad \text{or} \quad x \leftarrow \alpha A^{-T}x,$$

where  $A$  is an  $n$  by  $n$  real triangular band matrix with  $k$  subdiagonals or superdiagonals,  $x$  is an  $n$ -element real vector and  $\alpha$  is a real scalar.  $A^{-T}$  denotes  $(A^T)^{-1}$  or equivalently  $(A^{-1})^T$ .

No test for singularity or near-singularity of  $A$  is included in this function. Such tests must be performed before calling this function.

### 4 References

Basic Linear Algebra Subprograms Technical (BLAST) Forum (2001) *Basic Linear Algebra Subprograms Technical (BLAST) Forum Standard* University of Tennessee, Knoxville, Tennessee <http://www.netlib.org/blas/blast-forum/blas-report.pdf>

### 5 Arguments

- 1: **order** – Nag\_OrderType *Input*  
*On entry:* the **order** argument specifies the two-dimensional storage scheme being used, i.e., row-major ordering or column-major ordering. C language defined storage is specified by **order** = Nag\_RowMajor. See Section 2.3.1.3 in How to Use the NAG Library and its Documentation for a more detailed explanation of the use of this argument.  
*Constraint:* **order** = Nag\_RowMajor or Nag\_ColMajor.
- 2: **uplo** – Nag\_UploType *Input*  
*On entry:* specifies whether  $A$  is upper or lower triangular.  
**uplo** = Nag\_Upper  
 $A$  is upper triangular.  
**uplo** = Nag\_Lower  
 $A$  is lower triangular.  
*Constraint:* **uplo** = Nag\_Upper or Nag\_Lower.

- 3:     **trans** – Nag\_TransType *Input*  
*On entry:* specifies the operation to be performed.  
**trans** = Nag\_NoTrans  
 $x \leftarrow \alpha A^{-1}x$ .  
**trans** = Nag\_Trans or Nag\_ConjTrans  
 $x \leftarrow \alpha A^{-T}x$ .  
*Constraint:* **trans** = Nag\_NoTrans, Nag\_Trans or Nag\_ConjTrans.
- 4:     **diag** – Nag\_DiagType *Input*  
*On entry:* specifies whether  $A$  has nonunit or unit diagonal elements.  
**diag** = Nag\_NonUnitDiag  
The diagonal elements are stored explicitly.  
**diag** = Nag\_UnitDiag  
The diagonal elements are assumed to be 1 and are not referenced.  
*Constraint:* **diag** = Nag\_NonUnitDiag or Nag\_UnitDiag.
- 5:     **n** – Integer *Input*  
*On entry:*  $n$ , the order of the matrix  $A$ .  
*Constraint:*  $n \geq 0$ .
- 6:     **k** – Integer *Input*  
*On entry:*  $k$ , the number of subdiagonals or superdiagonals of the matrix  $A$ .  
*Constraint:*  $k \geq 0$ .
- 7:     **alpha** – double *Input*  
*On entry:* the scalar  $\alpha$ .
- 8:     **ab**[*dim*] – const double *Input*  
**Note:** the dimension, *dim*, of the array **ab** must be at least  $\max(1, \mathbf{pdab} \times \mathbf{n})$ .  
*On entry:* the  $n$  by  $n$  triangular band matrix  $A$ .  
This is stored as a notional two-dimensional array with row elements or column elements stored contiguously. The storage of elements of  $A_{ij}$ , depends on the **order** and **uplo** arguments as follows:  
if **order** = Nag\_ColMajor and **uplo** = Nag\_Upper,  
 $A_{ij}$  is stored in **ab**[ $k + i - j + (j - 1) \times \mathbf{pdab}$ ], for  $j = 1, \dots, n$  and  $i = \max(1, j - k), \dots, j$ ;  
if **order** = Nag\_ColMajor and **uplo** = Nag\_Lower,  
 $A_{ij}$  is stored in **ab**[ $i - j + (j - 1) \times \mathbf{pdab}$ ], for  $j = 1, \dots, n$  and  $i = j, \dots, \min(n, j + k)$ ;  
if **order** = Nag\_RowMajor and **uplo** = Nag\_Upper,  
 $A_{ij}$  is stored in **ab**[ $j - i + (i - 1) \times \mathbf{pdab}$ ], for  $i = 1, \dots, n$  and  $j = i, \dots, \min(n, i + k)$ ;  
if **order** = Nag\_RowMajor and **uplo** = Nag\_Lower,  
 $A_{ij}$  is stored in **ab**[ $k + j - i + (i - 1) \times \mathbf{pdab}$ ], for  $i = 1, \dots, n$  and  $j = \max(1, i - k), \dots, i$ .  
If **diag** = Nag\_UnitDiag, the diagonal elements of AB are assumed to be 1, and are not referenced.

- 9: **pdab** – Integer *Input*  
*On entry:* the stride separating row or column elements (depending on the value of **order**) of the matrix *A* in the array **ab**.  
*Constraint:* **pdab**  $\geq$  **k** + 1.
- 10: **x[dim]** – double *Input/Output*  
**Note:** the dimension, *dim*, of the array **x** must be at least  $\max(1, 1 + (\mathbf{n} - 1)|\mathbf{incx}|)$ .  
*On entry:* the right-hand side vector *b*.  
*On exit:* the solution vector *x*.
- 11: **incx** – Integer *Input*  
*On entry:* the increment in the subscripts of **x** between successive elements of *x*.  
*Constraint:* **incx**  $\neq$  0.
- 12: **fail** – NagError \* *Input/Output*  
The NAG error argument (see Section 2.7 in How to Use the NAG Library and its Documentation).

## 6 Error Indicators and Warnings

### NE\_ALLOC\_FAIL

Dynamic memory allocation failed.

See Section 2.3.1.2 in How to Use the NAG Library and its Documentation for further information.

### NE\_BAD\_PARAM

On entry, argument  $\langle value \rangle$  had an illegal value.

### NE\_INT

On entry, **incx** =  $\langle value \rangle$ .

Constraint: **incx**  $\neq$  0.

On entry, **k** =  $\langle value \rangle$ .

Constraint: **k**  $\geq$  0.

On entry, **n** =  $\langle value \rangle$ .

Constraint: **n**  $\geq$  0.

### NE\_INT\_2

On entry, **pdab** =  $\langle value \rangle$ , **k** =  $\langle value \rangle$ .

Constraint: **pdab**  $\geq$  **k** + 1.

### NE\_INTERNAL\_ERROR

An unexpected error has been triggered by this function. Please contact NAG.

See Section 2.7.6 in How to Use the NAG Library and its Documentation for further information.

### NE\_NO\_LICENCE

Your licence key may have expired or may not have been installed correctly.

See Section 2.7.5 in How to Use the NAG Library and its Documentation for further information.

## 7 Accuracy

The BLAS standard requires accurate implementations which avoid unnecessary over/underflow (see Section 2.7 of Basic Linear Algebra Subprograms Technical (BLAST) Forum (2001)).

## 8 Parallelism and Performance

nag\_dtbsv (f16pkc) is not threaded in any implementation.

## 9 Further Comments

None.

## 10 Example

This example solves the real triangular band system of linear equations  $Ax = y$ , where  $A$  is the 4 by 4 triangular matrix given with one subdiagonal given by

$$A = \begin{pmatrix} -4.16 & & & \\ -2.25 & 4.78 & & \\ & 5.86 & 6.32 & \\ & & -4.82 & 0.16 \end{pmatrix}$$

and where

$$y = (-16.64, -13.78, 13.10, -14.14)^T.$$

$A$  is stored in array **ab** using banded storage format and  $y$  is stored in array **x**. nag\_dtbsv (f16pkc) returns the solution in **x**.

### 10.1 Program Text

```
/* nag_dtbsv (f16pkc) Example Program.
 *
 * NAGPRODCODE Version.
 *
 * Copyright 2016 Numerical Algorithms Group.
 *
 * Mark 26, 2016.
 */

#include <stdio.h>
#include <nag.h>
#include <nag_stdlib.h>
#include <nagf16.h>

int main(void)
{
    /* Scalars */
    double alpha;
    Integer exit_status, i, incx, j, kd, n, pdab, xlen;

    /* Arrays */
    double *ab = 0, *x = 0;
    char nag_enum_arg[40];

    /* Nag Types */
    NagError fail;
    Nag_OrderType order;
    Nag_TransType trans;
    Nag_UploType uplo;
    Nag_DiagType diag;

#ifdef NAG_COLUMN_MAJOR
```

```

#define AB_UPPER(I, J) ab[(J-1)*pdab + kd + I - J]
#define AB_LOWER(I, J) ab[(J-1)*pdab + I - J]
    order = Nag_ColMajor;
#else
#define AB_UPPER(I, J) ab[(I-1)*pdab + J - I]
#define AB_LOWER(I, J) ab[(I-1)*pdab + kd + J - I]
    order = Nag_RowMajor;
#endif

    exit_status = 0;
    INIT_FAIL(fail);

    printf("nag_dtbsv (f16pkc) Example Program Results\n\n");

    /* Skip heading in data file */
#ifdef _WIN32
    scanf_s("%*[\n] ");
#else
    scanf("%*[\n] ");
#endif

    /* Read the problem dimensions */
#ifdef _WIN32
    scanf_s("%" NAG_IFMT "%" NAG_IFMT "%*[\n] ", &n, &kd);
#else
    scanf("%" NAG_IFMT "%" NAG_IFMT "%*[\n] ", &n, &kd);
#endif

    /* Read the uplo storage parameter */
#ifdef _WIN32
    scanf_s("%39s%*[\n] ", nag_enum_arg, (unsigned)_countof(nag_enum_arg));
#else
    scanf("%39s%*[\n] ", nag_enum_arg);
#endif
    /* nag_enum_name_to_value (x04nac).
     * Converts NAG enum member name to value
     */
    uplo = (Nag_UploType) nag_enum_name_to_value(nag_enum_arg);
    /* Read the transpose parameter */
#ifdef _WIN32
    scanf_s("%39s%*[\n] ", nag_enum_arg, (unsigned)_countof(nag_enum_arg));
#else
    scanf("%39s%*[\n] ", nag_enum_arg);
#endif
    /* nag_enum_name_to_value (x04nac), see above. */
    trans = (Nag_TransType) nag_enum_name_to_value(nag_enum_arg);
    /* Read the unit-diagonal parameter */
#ifdef _WIN32
    scanf_s("%39s%*[\n] ", nag_enum_arg, (unsigned)_countof(nag_enum_arg));
#else
    scanf("%39s%*[\n] ", nag_enum_arg);
#endif
    /* nag_enum_name_to_value (x04nac), see above. */
    diag = (Nag_DiagType) nag_enum_name_to_value(nag_enum_arg);

    /* Read scalar parameters */
#ifdef _WIN32
    scanf_s("%lf%*[\n] ", &alpha);
#else
    scanf("%lf%*[\n] ", &alpha);
#endif
    /* Read increment parameter */
#ifdef _WIN32
    scanf_s("%" NAG_IFMT "%*[\n] ", &incx);
#else
    scanf("%" NAG_IFMT "%*[\n] ", &incx);
#endif

    pdab = kd + 1;
    xlen = MAX(1, 1 + (n - 1) * ABS(incx));

```

```

if (n > 0) {
    /* Allocate memory */
    if (!(ab = NAG_ALLOC(pdab * n, double)) || !(x = NAG_ALLOC(xlen, double)))
    {
        printf("Allocation failure\n");
        exit_status = -1;
        goto END;
    }
}
else {
    printf("Invalid n\n");
    exit_status = 1;
    return exit_status;
}

/* Input matrix AB and vector x */

if (uplo == Nag_Upper) {
    for (i = 1; i <= n; ++i) {
        if (diag == Nag_NonUnitDiag)
#ifdef _WIN32
            scanf_s("%lf", &AB_UPPER(i, i));
#else
            scanf("%lf", &AB_UPPER(i, i));
#endif
        for (j = i + 1; j <= MIN(i + kd, n); ++j)
#ifdef _WIN32
            scanf_s("%lf", &AB_UPPER(i, j));
#else
            scanf("%lf", &AB_UPPER(i, j));
#endif
    }
#ifdef _WIN32
    scanf_s("%*[\n] ");
#else
    scanf("%*[\n] ");
#endif
    }
    else {
        for (i = 1; i <= n; ++i) {
            for (j = MAX(1, i - kd); j < i; ++j)
#ifdef _WIN32
                scanf_s("%lf", &AB_LOWER(i, j));
#else
                scanf("%lf", &AB_LOWER(i, j));
#endif
            if (diag == Nag_NonUnitDiag)
#ifdef _WIN32
                scanf_s("%lf", &AB_LOWER(i, i));
#else
                scanf("%lf", &AB_LOWER(i, i));
#endif
        }
#ifdef _WIN32
        scanf_s("%*[\n] ");
#else
        scanf("%*[\n] ");
#endif
    }
    for (i = 0; i < xlen; ++i)
#ifdef _WIN32
        scanf_s("%lf%*[\n] ", &x[i]);
#else
        scanf("%lf%*[\n] ", &x[i]);
#endif

    /* nag_dtbsv (f16pkc).
     * Solution of real triangular band system of linear equations.
     */
    nag_dtbsv(order, uplo, trans, diag, n, kd, alpha, ab, pdab, x, incx, &fail);

```

```

    if (fail.code != NE_NOERROR) {
        printf("Error from nag_dtbsv (f16pkc).\n%s\n", fail.message);
        exit_status = 1;
        goto END;
    }

    /* Print output vector x */
    printf("%s\n", " Solution x:");
    for (i = 0; i < xlen; ++i) {
        printf("%11f\n", x[i]);
    }

END:
    NAG_FREE(ab);
    NAG_FREE(x);

    return exit_status;
}

```

## 10.2 Program Data

```

nag_dtbsv (f16pkc) Example Program Data
  4  1                               :Values of n and kd
  Nag_Lower                          :Storage of A
  Nag_NoTrans                        :Transpose A?
  Nag_NonUnitDiag                    :Unit diagonal elements?
  1.0                                :Value of alpha
  1                                  :Value of incx
-4.16
-2.25    4.78
          5.86    6.32
          -4.82    0.16    :End of matrix A
-16.64
-13.78
 13.10
-14.14                                :End of vector x

```

## 10.3 Program Results

nag\_dtbsv (f16pkc) Example Program Results

```

Solution x:
  4.000000
 -1.000000
  3.000000
  2.000000

```

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