

# NAG Library Function Document

## nag\_superlu\_diagnostic\_lu (f11mmc)

### 1 Purpose

nag\_superlu\_diagnostic\_lu (f11mmc) computes the reciprocal pivot growth factor of an  $LU$  factorization of a real sparse matrix in compressed column (Harwell–Boeing) format.

### 2 Specification

```
#include <nag.h>
#include <nagf11.h>

void nag_superlu_diagnostic_lu (Integer n, const Integer icolzp[],
    const double a[], const Integer iprm[], const Integer il[],
    const double lval[], const Integer iu[], const double uval[],
    double *rpg, NagError *fail)
```

### 3 Description

nag\_superlu\_diagnostic\_lu (f11mmc) computes the reciprocal pivot growth factor  $\max_j \left( \|A_j\|_\infty / \|U_j\|_\infty \right)$  from the columns  $A_j$  and  $U_j$  of an  $LU$  factorization of the matrix  $A$ ,  $P_r A P_c = LU$  where  $P_r$  is a row permutation matrix,  $P_c$  is a column permutation matrix,  $L$  is unit lower triangular and  $U$  is upper triangular as computed by nag\_superlu\_lu\_factorize (f11mcc).

### 4 References

None.

### 5 Arguments

- 1: **n** – Integer *Input*  
*On entry:*  $n$ , the order of the matrix  $A$ .  
*Constraint:*  $n \geq 0$ .
- 2: **icolzp**[ $dim$ ] – const Integer *Input*  
**Note:** the dimension,  $dim$ , of the array **icolzp** must be at least  $n + 1$ .  
*On entry:* **icolzp**[ $i - 1$ ] contains the index in  $A$  of the start of a new column. See Section 2.1.3 in the f11 Chapter Introduction.
- 3: **a**[ $dim$ ] – const double *Input*  
**Note:** the dimension,  $dim$ , of the array **a** must be at least **icolzp**[ $n$ ] – 1, the number of nonzeros of the sparse matrix  $A$ .  
*On entry:* the array of nonzero values in the sparse matrix  $A$ .
- 4: **iprm**[ $7 \times n$ ] – const Integer *Input*  
*On entry:* the column permutation which defines  $P_c$ , the row permutation which defines  $P_r$ , plus associated data structures as computed by nag\_superlu\_lu\_factorize (f11mcc).

- 5: **il**[*dim*] – const Integer *Input*  
**Note:** the dimension, *dim*, of the array **il** must be at least as large as the dimension of the array of the same name in nag\_superlu\_lu\_factorize (f11mec).  
*On entry:* records the sparsity pattern of matrix *L* as computed by nag\_superlu\_lu\_factorize (f11mec).
- 6: **lval**[*dim*] – const double *Input*  
**Note:** the dimension, *dim*, of the array **lval** must be at least as large as the dimension of the array of the same name in nag\_superlu\_lu\_factorize (f11mec).  
*On entry:* records the nonzero values of matrix *L* and some nonzero values of matrix *U* as computed by nag\_superlu\_lu\_factorize (f11mec).
- 7: **iu**[*dim*] – const Integer *Input*  
**Note:** the dimension, *dim*, of the array **iu** must be at least as large as the dimension of the array of the same name in nag\_superlu\_lu\_factorize (f11mec).  
*On entry:* records the sparsity pattern of matrix *U* as computed by nag\_superlu\_lu\_factorize (f11mec).
- 8: **uval**[*dim*] – const double *Input*  
**Note:** the dimension, *dim*, of the array **uval** must be at least as large as the dimension of the array of the same name in nag\_superlu\_lu\_factorize (f11mec).  
*On entry:* records some nonzero values of matrix *U* as computed by nag\_superlu\_lu\_factorize (f11mec).
- 9: **rpg** – double \* *Output*  
*On exit:* the reciprocal pivot growth factor  $\max_j \left( \|A_j\|_\infty / \|U_j\|_\infty \right)$ . If the reciprocal pivot growth factor is much less than 1, the stability of the *LU* factorization may be poor.
- 10: **fail** – NagError \* *Input/Output*  
The NAG error argument (see Section 2.7 in How to Use the NAG Library and its Documentation).

## 6 Error Indicators and Warnings

### NE\_ALLOC\_FAIL

Dynamic memory allocation failed.

See Section 2.3.1.2 in How to Use the NAG Library and its Documentation for further information.

### NE\_BAD\_PARAM

On entry, argument  $\langle value \rangle$  had an illegal value.

### NE\_INT

On entry, **n** =  $\langle value \rangle$ .

Constraint: **n**  $\geq 0$ .

### NE\_INTERNAL\_ERROR

An internal error has occurred in this function. Check the function call and any array sizes. If the call is correct then please contact NAG for assistance.

An unexpected error has been triggered by this function. Please contact NAG.  
See Section 2.7.6 in How to Use the NAG Library and its Documentation for further information.

#### NE\_INVALID\_PERM\_COL

Incorrect column permutations in array **iprm**.

#### NE\_NO\_LICENCE

Your licence key may have expired or may not have been installed correctly.  
See Section 2.7.5 in How to Use the NAG Library and its Documentation for further information.

## 7 Accuracy

Not applicable.

## 8 Parallelism and Performance

nag\_superlu\_diagnostic\_lu (f11mmc) is not threaded in any implementation.

## 9 Further Comments

If the reciprocal pivot growth factor, **rpg**, is much less than 1, then the factorization of the matrix  $A$  could be poor. This means that using the factorization to obtain solutions to a linear system, forward error bounds and estimates of the condition number could be unreliable. Consider increasing the **thresh** argument in the call to nag\_superlu\_lu\_factorize (f11mcc).

## 10 Example

To compute the reciprocal pivot growth for the factorization of the matrix  $A$ , where

$$A = \begin{pmatrix} 2.00 & 1.00 & 0 & 0 & 0 \\ 0 & 0 & 1.00 & -1.00 & 0 \\ 4.00 & 0 & 1.00 & 0 & 1.00 \\ 0 & 0 & 0 & 1.00 & 2.00 \\ 0 & -2.00 & 0 & 0 & 3.00 \end{pmatrix}.$$

In this case, it should be equal to 1.0.

### 10.1 Program Text

```
/* nag_superlu_diagnostic_lu (f11mmc) Example Program.
 *
 * NAGPRODCODE Version.
 *
 * Copyright 2016 Numerical Algorithms Group.
 *
 * Mark 26, 2016.
 */

#include <stdio.h>
#include <nag.h>
#include <nag_stdlib.h>
#include <nagf11.h>

int main(void)
{
    double flop, rpg, thresh;
    Integer exit_status = 0, i, n, nnz, nnzl, nnzu, nzlmax, nzlmax, nzumx;
    double *a = 0, *lval = 0, *uval = 0;
    Integer *icolzp = 0, *il = 0, *iprm = 0, *irowix = 0;
    Integer *iu = 0;
    /* Nag types */
```

```

Nag_ColumnPermutationType ispec;
NagError fail;

INIT_FAIL(fail);

printf("nag_superlu_diagnostic_lu (f11mmc) Example Program Results\n\n");
/* Skip heading in data file */
#ifdef _WIN32
scanf_s("%*[\n] ");
#else
scanf("%*[\n] ");
#endif
/* Read order of matrix */
#ifdef _WIN32
scanf_s("%" NAG_IFMT "%*[\n] ", &n);
#else
scanf("%" NAG_IFMT "%*[\n] ", &n);
#endif
/* Read the matrix A */
if (!(icolzp = NAG_ALLOC(n + 1, Integer)))
{
printf("Allocation failure\n");
exit_status = -1;
goto END;
}
for (i = 1; i <= n + 1; ++i)
#ifdef _WIN32
scanf_s("%" NAG_IFMT "%*[\n] ", &icolzp[i - 1]);
#else
scanf("%" NAG_IFMT "%*[\n] ", &icolzp[i - 1]);
#endif
nnz = icolzp[n] - 1;
/* Allocate memory */
if (!(irowix = NAG_ALLOC(nnz, Integer)) ||
!(a = NAG_ALLOC(nnz, double)) ||
!(il = NAG_ALLOC(7 * n + 8 * nnz + 4, Integer)) ||
!(iu = NAG_ALLOC(2 * n + 8 * nnz + 1, Integer)) ||
!(uval = NAG_ALLOC(8 * nnz, double)) ||
!(lval = NAG_ALLOC(8 * nnz, double)) ||
!(iprm = NAG_ALLOC(7 * n, Integer)))
{
printf("Allocation failure\n");
exit_status = -1;
goto END;
}
for (i = 1; i <= nnz; ++i)
#ifdef _WIN32
scanf_s("%lf%" NAG_IFMT "%*[\n] ", &a[i - 1], &irowix[i - 1]);
#else
scanf("%lf%" NAG_IFMT "%*[\n] ", &a[i - 1], &irowix[i - 1]);
#endif
/* Calculate COLAMD permutation */
ispec = Nag_Sparse_Colamd;
/* nag_superlu_column_permutation (f11mdc).
* Real sparse nonsymmetric linear systems, setup for
* nag_superlu_lu_factorize (f11mec)
*/
nag_superlu_column_permutation(ispec, n, icolzp, irowix, iprm, &fail);
if (fail.code != NE_NOERROR) {
printf("Error from nag_superlu_column_permutation (f11mdc).\n%s\n",
fail.message);
exit_status = 1;
goto END;
}

/* Factorise */
thresh = 1.;
nzlmx = 8 * nnz;
nzlumx = 8 * nnz;
nzumx = 8 * nnz;
/* nag_superlu_lu_factorize (f11mec).

```

```

    * LU factorization of real sparse matrix
    */
nag_superlu_lu_factorize(n, irowix, a, iprm, thresh, nzlmx, &nzlumx, nzumx,
                        il, lval, iu, uval, &nnzl, &nnzu, &flop, &fail);
if (fail.code != NE_NOERROR) {
    printf("Error from nag_superlu_lu_factorize (f11mec).\n%s\n",
           fail.message);
    exit_status = 1;
    goto END;
}

/* Calculate reciprocal pivot growth */
/* nag_superlu_diagnostic_lu (f11mmc).
 * Real sparse nonsymmetric linear systems, diagnostic for
 * nag_superlu_lu_factorize (f11mec)
 */
nag_superlu_diagnostic_lu(n, icolzp, a, iprm, il, lval, iu, uval, &rpg,
                          &fail);
if (fail.code != NE_NOERROR) {
    printf("Error from nag_superlu_diagnostic_lu (f11mmc).\n%s\n",
           fail.message);
    exit_status = 1;
    goto END;
}

/* Output result */
printf("\n");
printf("%s\n%7.3f\n", "Reciprocal pivot growth", rpg);

END:
    NAG_FREE(a);
    NAG_FREE(lval);
    NAG_FREE(uval);
    NAG_FREE(icolzp);
    NAG_FREE(il);
    NAG_FREE(iprm);
    NAG_FREE(irowix);
    NAG_FREE(iu);

    return exit_status;
}

```

## 10.2 Program Data

nag\_superlu\_diagnostic\_lu (f11mmc) Example Program Data

```

5  n
1
3
5
7
9
12  icolzp(i) i=0..n
2.  1
4.  3
1.  1
-2. 5
1.  2
1.  3
-1. 2
1.  4
1.  3
2.  4
3.  5      a(i) irowix(i) i=0..nnz-1

```

### 10.3 Program Results

nag\_superlu\_diagnostic\_lu (f11mmc) Example Program Results

```
Reciprocal pivot growth  
1.000
```

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