

NAG Library Function Document

nag_superlu_column_permutation (f11mdc)

1 Purpose

nag_superlu_column_permutation (f11mdc) computes a column permutation suitable for LU factorization (by nag_superlu_lu_factorize (f11mec)) of a real sparse matrix in compressed column (Harwell–Boeing) format and applies it to the matrix. This function must be called prior to nag_superlu_lu_factorize (f11mec).

2 Specification

```
#include <nag.h>
#include <nagf11.h>

void nag_superlu_column_permutation (Nag_ColumnPermutationType spec,
    Integer n, const Integer icolzp[], const Integer irowix[],
    Integer iprm[], NagError *fail)
```

3 Description

Given a sparse matrix in compressed column (Harwell–Boeing) format A and a choice of column permutation schemes, the function computes those data structures that will be needed by the LU factorization function nag_superlu_lu_factorize (f11mec) and associated functions nag_superlu_diagnostic_lu (f11mmc), nag_superlu_solve_lu (f11mfc) and nag_superlu_refine_lu (f11mhc). The column permutation choices are:

original order (that is, no permutation);

user-supplied permutation;

a permutation, computed by the function, designed to minimize fill-in during the LU factorization.

The algorithm for this computed permutation is based on the approximate minimum degree column ordering algorithm COLAMD. The computed permutation is not sensitive to the magnitude of the nonzero values of A .

4 References

Amestoy P R, Davis T A and Duff I S (1996) An approximate minimum degree ordering algorithm *SIAM J. Matrix Anal. Appl.* **17** 886–905

Gilbert J R and Larimore S I (2004) A column approximate minimum degree ordering algorithm *ACM Trans. Math. Software* **30**, 3 353–376

Gilbert J R, Larimore S I and Ng E G (2004) Algorithm 836: COLAMD, an approximate minimum degree ordering algorithm *ACM Trans. Math. Software* **30**, 3 377–380

5 Arguments

- 1: **spec** – Nag_ColumnPermutationType *Input*
On entry: indicates the permutation to be applied.
- spec** = Nag_Sparse_Identity
 The identity permutation is used (i.e., the columns are not permuted).
- spec** = Nag_Sparse_User
 The permutation in the **iprm** array is used, as supplied by you.

spec = Nag_Sparse_Colamd

The permutation computed by the COLAMD algorithm is used

Constraint: **spec** = Nag_Sparse_Identity, Nag_Sparse_User or Nag_Sparse_Colamd.

- 2: **n** – Integer *Input*
On entry: n , the order of the matrix A .
Constraint: $n \geq 0$.
- 3: **icolzp**[dim] – const Integer *Input*
Note: the dimension, dim , of the array **icolzp** must be at least $n + 1$.
On entry: **icolzp**[$i - 1$] contains the index in A of the start of a new column. See Section 2.1.3 in the f11 Chapter Introduction.
- 4: **irowix**[dim] – const Integer *Input*
Note: the dimension, dim , of the array **irowix** must be at least **icolzp**[n] – 1, the number of nonzeros of the sparse matrix A .
On entry: **irowix**[$i - 1$] contains the row index in A for element $A(i)$. See Section 2.1.3 in the f11 Chapter Introduction.
- 5: **iprm**[$7 \times n$] – Integer *Input/Output*
On entry: the first n entries contain the column permutation supplied by you. This will be used if **spec** = Nag_Sparse_User, and ignored otherwise. If used, it must consist of a permutation of all the integers in the range $[0, (n - 1)]$, the leftmost column of the matrix A denoted by 0 and the rightmost by $n - 1$. Labelling columns in this way, **iprm**[i] = j means that column $i - 1$ of A is in position j in AP_c , where $P_rAP_c = LU$ expresses the factorization to be performed.
On exit: a new permutation is returned in the first n entries. The rest of the array contains data structures that will be used by other functions. The function computes the column elimination tree for A and a post-order permutation on the tree. It then compounds the **iprm** permutation given or computed by the COLAMD algorithm with the post-order permutation. This array is needed by the LU factorization function nag_superlu_lu_factorize (f11mec) and associated functions nag_superlu_solve_lu (f11mfc), nag_superlu_refine_lu (f11mhc) and nag_superlu_diagnostic_lu (f11mmc) and should be passed to them unchanged.
- 6: **fail** – NagError * *Input/Output*
The NAG error argument (see Section 2.7 in How to Use the NAG Library and its Documentation).

6 Error Indicators and Warnings

NE_ALG_FAIL

COLAMD algorithm failed.

NE_ALLOC_FAIL

Dynamic memory allocation failed.

See Section 2.3.1.2 in How to Use the NAG Library and its Documentation for further information.

NE_BAD_PARAM

On entry, argument $\langle value \rangle$ had an illegal value.

NE_INT

On entry, **n** = $\langle value \rangle$.
 Constraint: **n** ≥ 0 .

NE_INTERNAL_ERROR

An internal error has occurred in this function. Check the function call and any array sizes. If the call is correct then please contact NAG for assistance.

An unexpected error has been triggered by this function. Please contact NAG.
 See Section 2.7.6 in How to Use the NAG Library and its Documentation for further information.

NE_INVALID_PERM_COL

Incorrect column permutations in array **iprm**.

NE_NO_LICENCE

Your licence key may have expired or may not have been installed correctly.
 See Section 2.7.5 in How to Use the NAG Library and its Documentation for further information.

NE_SPARSE_COL

Incorrect specification of argument **icolzp**.

NE_SPARSE_ROW

Incorrect specification of argument **irowix**.

7 Accuracy

Not applicable. This computation does not use floating-point numbers.

8 Parallelism and Performance

`nag_superlu_column_permutation` (f11mdc) is threaded by NAG for parallel execution in multithreaded implementations of the NAG Library.

Please consult the x06 Chapter Introduction for information on how to control and interrogate the OpenMP environment used within this function. Please also consult the Users' Note for your implementation for any additional implementation-specific information.

9 Further Comments

We recommend calling this function with **spec** = Nag_Sparse_Colamd before calling `nag_superlu_lu_factorize` (f11mec). The COLAMD algorithm computes a sparsity-preserving permutation P_c solely from the pattern of A such that the LU factorization $P_r A P_c = LU$ remains as sparse as possible, regardless of the subsequent choice of P_r . The algorithm takes advantage of the existence of super-columns (columns with the same sparsity pattern) to reduce running time.

10 Example

This example computes a sparsity preserving column permutation for the LU factorization of the matrix A , where

$$A = \begin{pmatrix} 2.00 & 1.00 & 0 & 0 & 0 \\ 0 & 0 & 1.00 & -1.00 & 0 \\ 4.00 & 0 & 1.00 & 0 & 1.00 \\ 0 & 0 & 0 & 1.00 & 2.00 \\ 0 & -2.00 & 0 & 0 & 3.00 \end{pmatrix}.$$

10.1 Program Text

```

/* nag_superlu_column_permutation (f11mdc) Example Program.
 *
 * NAGPRODCODE Version.
 *
 * Copyright 2016 Numerical Algorithms Group.
 *
 * Mark 26, 2016.
 */

#include <stdio.h>
#include <nag.h>
#include <nag_stdlib.h>
#include <nagf11.h>

int main(void)
{
    Integer exit_status = 0, i, n, nnz;
    Integer *icolzp = 0, *iprm = 0, *irowix = 0;
    /* Nag types */
    Nag_ColumnPermutationType ispec;
    NagError fail;

    INIT_FAIL(fail);

    printf("nag_superlu_column_permutation (f11mdc) Example Program Results"
           "\n\n");
    /* Skip heading in data file */
#ifdef _WIN32
    scanf_s("%*[\n] ");
#else
    scanf("%*[\n] ");
#endif
    /* Read order of matrix */
#ifdef _WIN32
    scanf_s("%" NAG_IFMT "%*[\n] ", &n);
#else
    scanf("%" NAG_IFMT "%*[\n] ", &n);
#endif
    if (!(icolzp = NAG_ALLOC(n + 1, Integer)))
    {
        printf("Allocation failure\n");
        exit_status = -1;
        goto END;
    }
    /* Read the matrix A */
#ifdef _WIN32
    for (i = 1; i <= n + 1; ++i)
        scanf_s("%" NAG_IFMT "%*[\n] ", &icolzp[i - 1]);
#else
    for (i = 1; i <= n + 1; ++i)
        scanf("%" NAG_IFMT "%*[\n] ", &icolzp[i - 1]);
#endif
    nnz = icolzp[n] - 1;
    if (!(irowix = NAG_ALLOC(nnz, Integer)) ||
        !(iprm = NAG_ALLOC(7 * n, Integer)))
    {
        printf("Allocation failure\n");
        exit_status = -1;
        goto END;
    }
#ifdef _WIN32
    for (i = 1; i <= nnz; ++i)
        scanf_s("%" NAG_IFMT "%*[\n] ", &irowix[i - 1]);
#else
    for (i = 1; i <= nnz; ++i)
        scanf("%" NAG_IFMT "%*[\n] ", &irowix[i - 1]);
#endif
    /* Calculate COLAMD permutation */
    ispec = Nag_Sparse_Colamd;

```

```

/* nag_superlu_column_permutation (f11mdc).
 * Real sparse nonsymmetric linear systems, setup for
 * nag_superlu_lu_factorize (f11mec)
 */
nag_superlu_column_permutation(ispec, n, icolzp, irowix, iprm, &fail);
if (fail.code != NE_NOERROR) {
    printf("Error from nag_superlu_column_permutation (f11mdc).\n%s\n",
           fail.message);
    exit_status = 1;
    goto END;
}

/* Output results */
printf("\n");
printf("%s\n", "COLAMD Permutation");
for (i = 1; i <= n; ++i)
    printf("%6" NAG_IFMT "%s", iprm[i - 1], i % 10 == 0
           || i == n ? "\n" : " ");

/* Calculate user permutation */
ispec = Nag_Sparse_User;
iprm[0] = 4;
iprm[1] = 3;
iprm[2] = 2;
iprm[3] = 1;
iprm[4] = 0;
/* nag_superlu_column_permutation (f11mdc), see above. */
nag_superlu_column_permutation(ispec, n, icolzp, irowix, iprm, &fail);
if (fail.code != NE_NOERROR) {
    printf("Error from nag_superlu_column_permutation (f11mdc).\n%s\n",
           fail.message);
    exit_status = 1;
    goto END;
}

/* Output results */
printf("\n");
printf("%s", "User Permutation");
printf("\n");
for (i = 1; i <= n; ++i)
    printf("%6" NAG_IFMT "%s", iprm[i - 1], i % 10 == 0
           || i == n ? "\n" : " ");

/* Calculate natural permutation */
ispec = Nag_Sparse_Identity;
/* nag_superlu_column_permutation (f11mdc), see above. */
nag_superlu_column_permutation(ispec, n, icolzp, irowix, iprm, &fail);
if (fail.code != NE_NOERROR) {
    printf("Error from nag_superlu_column_permutation (f11mdc).\n%s\n",
           fail.message);
    exit_status = 1;
    goto END;
}

/* Output results */
printf("\n");
printf("%s\n", "Natural Permutation");
for (i = 1; i <= n; ++i)
    printf("%6" NAG_IFMT "%s", iprm[i - 1], i % 10 == 0
           || i == n ? "\n" : " ");
printf("\n");

END:
NAG_FREE(icolzp);
NAG_FREE(iprm);
NAG_FREE(irowix);

return exit_status;
}

```

10.2 Program Data

nag_superlu_column_permutation (f11mdc) Example Program Data

```

5      n
1
3
5
7
9
12     icolzp(i) i=0..n
1
3
1
5
2
3
2
4
3
4
5      irowix(i) i=0..nnz-1

```

10.3 Program Results

nag_superlu_column_permutation (f11mdc) Example Program Results

```

COLAMD Permutation
  1      0      4      3      2

User Permutation
  4      3      2      1      0

Natural Permutation
  0      1      2      3      4

```
